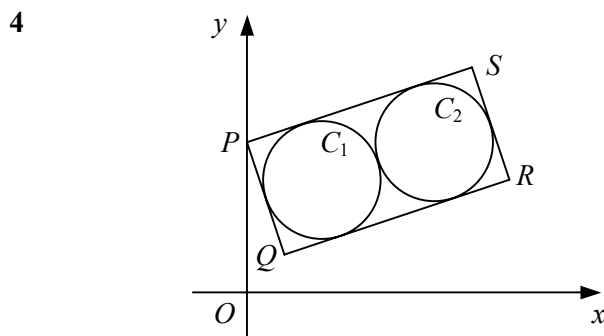


- 1 Write down an equation of the circle with the given centre and radius in each case.
- a** centre (0, 0) radius 5 **b** centre (1, 3) radius 2 **c** centre (4, -6) radius 1
d centre (-1, -8) radius 3 **e** centre $(-\frac{1}{2}, \frac{1}{2})$ radius $\frac{1}{2}$ **f** centre (-3, 9) radius $2\sqrt{3}$
- 2 Write down the coordinates of the centre and the radius of each of the following circles.
- a** $x^2 + y^2 = 16$ **b** $(x - 6)^2 + (y - 1)^2 = 81$ **c** $(x + 1)^2 + (y - 4)^2 = 121$
d $(x - 7)^2 + y^2 = 0.09$ **e** $(x + 2)^2 + (y + 5)^2 = 32$ **f** $(x - 8)^2 + (y + 9)^2 = 108$
- 3 Find the coordinates of the centre and the radius of each of the following circles.
- a** $x^2 + y^2 - 4y + 3 = 0$ **b** $x^2 + y^2 - 2x - 10y - 23 = 0$
c $x^2 + y^2 + 12x - 8y + 36 = 0$ **d** $x^2 + y^2 - 2x + 16y = 35$
e $x^2 + y^2 = 8x - 6y$ **f** $x^2 + y^2 + 10x - 2y - 19 = 0$
g $4x^2 + 4y^2 - 4x - 24y + 1 = 0$ **h** $9x^2 + 9y^2 + 6x - 24y + 8 = 0$
- 4 Find an equation of the circle
- a** with centre (1, -2) which passes through the point (4, 2),
b with centre (-5, 7) which passes through the point (0, 5).
- 5 Find an equation of the circle in which AB is a diameter in each case.
- a** $A(1, -2)$ $B(3, -2)$ **b** $A(-7, 2)$ $B(1, 8)$ **c** $A(1, 1)$ $B(4, 0)$
- 6 The points $P(0, 1)$, $Q(3, 10)$ and $R(6, 9)$ all lie on circle C .
- a** Show that $\angle PQR$ is a right-angle.
b Hence, show that C has the equation $x^2 + y^2 - 6x - 10y + 9 = 0$.
- 7 Find in each case whether the given point lies inside, outside or on the given circle.
- a** (0, -9) $x^2 + y^2 = 64$ **b** (4, 7) $x^2 + y^2 - 2x - 6y - 26 = 0$
c (7, -3) $x^2 + y^2 + 10x - 4y = 140$ **d** (-4, 1) $x^2 + y^2 + 2x + 8y - 13 = 0$
- 8 The point P lies on the circle with equation $x^2 + y^2 + 12x - 6y + 27 = 0$ and the point Q has coordinates (8, 1). Find the minimum length of PQ giving your answer in the form $k\sqrt{2}$.
- 9 Find an equation of the circle which crosses the x -axis at the points (2, 0) and (8, 0) and touches the y -axis at the point (0, 4).
- 10 Given that the circle with equation $x^2 + y^2 + 8x - 12y + k = 0$ does not touch or cross either of the coordinate axes, find the set of possible values of the constant k .
- 11 The circle C passes through the points P , Q and R with coordinates (-2, -2), (2, -4) and (7, 1) respectively.
- a** Find an equation of the perpendicular bisector of the points P and Q .
b Find the coordinates of the centre of C .
c Find an equation of C .

- 12 The circle C has the equation $x^2 + y^2 - 4x - 4y - 28 = 0$.
- a Find the distance of the point $A(10, 8)$ from the centre of C .
The tangent to C at the point B passes through A .
- b Find the length AB .
- 13 A circle has the equation $x^2 + y^2 + 6x - 2y = 0$ and passes through the point P .
Given that the tangent to the circle at P passes through the point $Q(2, 6)$, find the exact length PQ in its simplest form.
- 14 The circle C has the equation $x^2 + y^2 - 6x - 10y + 16 = 0$ and passes through the point $A(6, 2)$.
- a Find the coordinates of the centre of C .
- b Find the gradient of the normal to the circle at A .
- c Find an equation of the normal to the circle at A .
- 15 Find an equation of
- a the normal to the circle with equation $x^2 + y^2 + 4x = 13$ at the point $(-1, 4)$,
- b the tangent to the circle with equation $x^2 + y^2 + 2x + 4y - 40 = 0$ at the point $(5, 1)$,
- c the tangent to the circle with equation $x^2 + y^2 - 10x + 4y + 4 = 0$ at the point $(2, 2)$.
- 16 Find the coordinates of the points where the circle with equation $x^2 + y^2 - 6x + 6y - 16 = 0$ intersects the coordinate axes.
- 17 Find in each case the coordinates of the points where the line l intersects the circle C .
- a $l: y = x - 4$ $C: x^2 + y^2 = 10$
- b $l: 3x + y = 17$ $C: x^2 + y^2 - 4x - 2y - 15 = 0$
- c $l: y = 2x + 2$ $C: 4x^2 + 4y^2 + 4x - 8y - 15 = 0$
- 18 The line with equation $y = 1 - x$ intersects the circle with equation $x^2 + y^2 + 6x + 2y = 27$ at the points A and B .
Find the length of the chord AB , giving your answer in the form $k\sqrt{2}$.
- 19 Show that the line with equation $y = 2x + 1$ is a tangent to the circle with equation $x^2 + y^2 - 8x - 8y + 27 = 0$ and find the coordinates of the point where they touch.
- 20 The line with equation $y = x + k$ is a tangent to the circle with equation $x^2 + y^2 + 6x - 8y + 17 = 0$.
Find the two possible values of k .
- 21 The line with equation $y = mx$ is a tangent to the circle with equation $x^2 + y^2 - 8x - 16y + 72 = 0$.
Find the two possible values of m .
- 22 The line with equation $2x + 3y = k$ is a tangent to the circle with equation $x^2 + y^2 + 6x + 4y = 0$.
Find the two possible values of k .
- 23 The circle with equation $x^2 + y^2 - 4x - 6y = 7$ crosses the y -axis at the points A and B .
- a Find the coordinates of the points A and B .
- b Find the coordinates of the point where the tangent to the circle at A intersects the tangent to the circle at B .

- 1 The circle C has centre $(3, -2)$ and radius 5.
 a Write down an equation of C in cartesian form.
 The line $y = 2x - 3$ intersects C at the points A and B .
 b Show that $AB = 4\sqrt{5}$.
- 2 The line AB is a diameter of circle C .
 Given that A has coordinates $(-5, 6)$ and B has coordinates $(3, 8)$, find
 a the coordinates of the centre of C ,
 b a cartesian equation for C ,
 c an equation of the tangent to C at A .
- 3 The circle C has equation $x^2 + y^2 + 8x - 16y + 62 = 0$.
 a Find the coordinates of the centre of C and the exact radius of C .
 The line l has equation $y = 2x + 1$.
 b Show that the minimum distance between l and C is $3(\sqrt{5} - \sqrt{2})$.

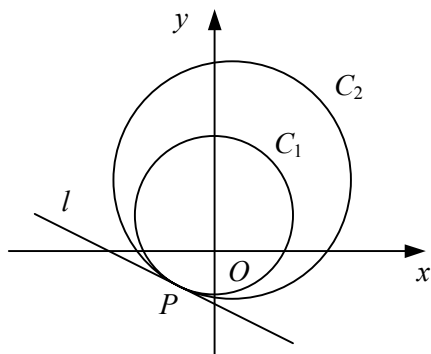


- The diagram shows rectangle $PQRS$ and circles C_1 and C_2 .
 Each circle touches the other circle and three sides of the rectangle. The coordinates of the corners of the rectangle are $P(0, 4)$, $Q(1, 1)$, $R(7, 3)$ and $S(6, 6)$.
- a Find the radius of C_1 .
 b Find the coordinates of the point where the two circles touch.
 c Show that C_1 has equation $2x^2 + 2y^2 - 8x - 12y + 21 = 0$.
- 5 The circle C touches the y -axis at the point $A(0, 3)$ and passes through the point $B(2, 7)$.
 a Find an equation of the perpendicular bisector of AB .
 b Find an equation for C .
 c Show that the tangent to C at B has equation

$$3x - 4y + 22 = 0$$
.
- 6 The point $P(x, y)$ moves such that its distance from the point $A(-3, 4)$ is twice its distance from the point $B(0, -2)$.
 Show that the locus of P is a circle and find the coordinates of the centre and the exact radius of this circle.

- 7 The points $P(-4, 9)$ and $Q(-2, -5)$ are such that PQ is a diameter of circle C .
- Find the coordinates of the centre of C .
 - Find an equation for C .
 - Show that the point $R(2, 7)$ lies on C .
 - Hence, state the size of $\angle PRQ$, giving a reason for your answer.

8



The diagram shows circles C_1 and C_2 , which both pass through the point P , and the common tangent to the circles at P , the line l .

Circle C_1 has the equation $x^2 + y^2 - 4y - 16 = 0$.

- Find the coordinates of the centre of C_1 .

Circle C_2 has the equation $x^2 + y^2 - 2x - 8y - 60 = 0$.

- Find an equation of the straight line passing through the centre of C_1 and the centre of C_2 .
- Find an equation of line l .

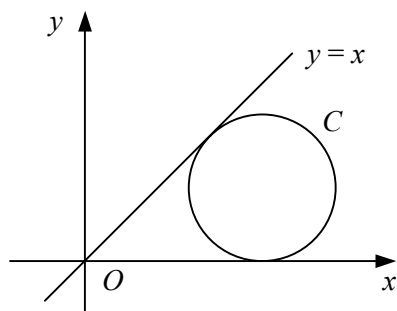
- 9 The circle C has equation $x^2 + y^2 - 8x + 4y + 12 = 0$.

- Find the coordinates of the centre of C and the radius of C .

The point P has coordinates $(3, 5)$ and the point Q lies on C .

- Find the largest and smallest values of the length PQ , giving your answers in the form $k\sqrt{2}$.
- Find the length of PQ correct to 3 significant figures when the line PQ is a tangent to C .

10



The diagram shows the circle C and the line $y = x$.

Given that circle C has centre (a, b) , where a and b are positive constants, and that C touches the x -axis,

- find a cartesian equation for C in terms of a and b .

Given also that the line $y = x$ is a tangent to C ,

- show that $a = (1 + \sqrt{2})b$.