

Integration - Edexcel Past Exam Questions **MARK SCHEME**

Question 1 : Jan 05 Q2

Question number	Scheme	Marks
	(i) (a) $15x^2 + 7$ (i) (b) $30x$ (ii) $x + 2x^{\frac{3}{2}} + x^{-1} + C$	M1 A1 A1 (3) B1ft (1) M1 A1 A1 A1 (4) 8
	(i) (a) A1: 2 terms correctly differentiated. A1: Fully correct. (ii) Allow any equivalent version of each term.	

Question 2 : Jan 05 Q9

Question number	Scheme	Marks
	(a) Gradient of tangent at P: $m = 4$, Grad. of normal $= -\frac{1}{m} \left(= -\frac{1}{4} \right)$ Equation of normal: $y - 4 = -\frac{1}{4}(x - 1)$ ($4y = -x + 17$) (b) $(3x - 1)^2 = 9x^2 - 6x + 1$ Integrate: $\frac{9x^3}{3} - \frac{6x^2}{2} + x (+C)$ Substitute (1, 4) to find $c = \dots$, $c = 3$ ($y = 3x^3 - 3x^2 + x + 3$) (c) Gradient of (tangent to) C is ≥ 0 Gradient of given line is < 0 (-2)	B1, M1 M1 A1 (4) B1 M1 A1ft M1, A1 (5) B1 B1 (2) 11
	(a) Using gradient of tangent is M0. (b) <u>Alternative:</u> $y = \frac{(3x - 1)^3}{9} (+C)$ M1 A1 (numerator) A1 (denominator) Substitute (1, 4) to find $c = \dots$, $c = \frac{28}{9}$ $\left(y = \frac{(3x - 1)^3}{9} + \frac{28}{9} \right)$ M1, A1	



Question 3 : June 05 Q2

Question number	Scheme	Marks
	<p>(a) $x \log 5 = \log 8, \quad x = \frac{\log 8}{\log 5}, \quad = 1.29$</p> <p>(b) $\log_2 \frac{x+1}{x} \quad (\text{or } \log_2 7x)$</p> <p>$\frac{x+1}{x} = 7 \quad x = \dots, \quad \frac{1}{6} \quad (\text{Allow } 0.167 \text{ or better})$</p>	<p>M1, A1, A1 (3)</p> <p>B1</p> <p>M1, A1 (3)</p> <p>6</p>
	<p>(a) Answer only 1.29 : Full marks. Answer only, which rounds to 1.29 (e.g. 1.292): M1 A1 A0 Answer only, which rounds to 1.3 : M1 A0 A0 Trial and improvement: Award marks as for “answer only”.</p> <p>(b) M1: Form (by legitimate log work) and solve an equation in x. Answer only: No marks unless verified (then full marks are available).</p>	

Question 4 : June 05 Q7

Question Number	Scheme	Marks
(a)	$(3 - \sqrt{x})^2 = 9 - 6\sqrt{x} + x$ $\div by \sqrt{x} \rightarrow 9x^{-\frac{1}{2}} - 6 + x^{\frac{1}{2}}$	M1 A1 c.s.o. (2)
(b)	$\int (9x^{-\frac{1}{2}} - 6 + x^{\frac{1}{2}}) dx = \frac{9x^{\frac{1}{2}}}{\frac{1}{2}} - 6x + \frac{x^{\frac{3}{2}}}{\frac{3}{2}} (+c)$ <p>use $y = \frac{2}{3}$ and $x = 1$: $\frac{2}{3} = 18 - 6 + \frac{2}{3} + c$</p> <p style="text-align: right;">$c = -12$</p> <p>So $y = 18x^{\frac{1}{2}} - 6x + \frac{2}{3}x^{\frac{3}{2}} - 12$</p>	M1 A2/1/0 M1 A1 c.s.o. A1f.t. (6) (8)
(a)	M1 Attempt to multiply out $(3 - \sqrt{x})^2$. Must have 3 or 4 terms, allow one sign error A1 cso Fully correct solution to printed answer. Penalise wrong working.	
(b)	1 st M1 Some correct integration: $x^n \rightarrow x^{n+1}$ A1 At least 2 correct unsimplified terms A2 All 3 terms correct (unsimplified) <p style="text-align: right;">Ignore + c</p> 2 nd M1 Use of $y = \frac{2}{3}$ and $x = 1$ to find c. No + c is M0. A1c.s.o. for -12. (o.e.) Award this mark if “ $c = -12$ ” stated i.e. not as part of an expression for y A1f.t. for 3 simplified x terms with $y = \dots$ and a numerical value for c. Follow through their value of c but it must be a number.	



Question 5 : Jan 06 Q4

Question number	Scheme	Marks
(a) $\frac{dy}{dx} = 4x + 18x^{-4}$	M1: $x^2 \rightarrow x$ or $x^{-3} \rightarrow x^{-4}$	M1 A1 (2)
(b) $\frac{2x^3}{3} - \frac{6x^{-2}}{-2} + C$	M1: $x^2 \rightarrow x^3$ or $x^{-3} \rightarrow x^{-2}$ or $+C$	M1 A1 A1 (3)
$\left(= \frac{2x^3}{3} + 3x^{-2} + C \right)$	First A1: $\frac{2x^3}{3} + C$ Second A1: $-\frac{6x^{-2}}{-2}$	Total 5 marks
<p>In both parts, accept any correct version, simplified or not. Accept $4x^1$ for $4x$.</p> <p><u>$+C$ in part (a) instead of part (b):</u> Penalise only once, so if otherwise correct scores M1 A0, M1 A1 A1.</p>		



Question 6 : Jan 06 Q8

Question number	Scheme	Marks
	$\frac{5x^2 + 2}{x^{\frac{1}{2}}} = 5x^{\frac{3}{2}} + 2x^{-\frac{1}{2}}$ <p>M1: One term correct.</p> <p>A1: Both terms correct, and no extra terms.</p> $f(x) = 3x + \frac{5x^{\frac{5}{2}}}{\left(\frac{5}{2}\right)} + \frac{2x^{\frac{1}{2}}}{\left(\frac{1}{2}\right)} (+C) \quad (+C \text{ not required here})$ <p>6 = 3 + 2 + 4 + C Use of $x = 1$ and $y = 6$ to form eqn. in C</p> <p>$C = -3$</p> $3x + 2x^{\frac{5}{2}} + 4x^{\frac{1}{2}} - 3 \quad (\text{simplified version required})$ <p>[or: $3x + 2\sqrt{x^5} + 4\sqrt{x} - 3$ or equiv.]</p>	<p>M1 A1</p> <p>M1 A1ft</p> <p>M1 A1cso</p> <p>A1 (ft C)</p> <p>(7)</p> <p>Total 7 marks</p>
	<p>For the integration:</p> <p>M1 requires evidence from just one term (e.g. $3 \rightarrow 3x$), but not just “+C”.</p> <p>A1ft requires correct integration of at least 3 terms, with at least one of these terms having a fractional power.</p> <p>For the final A1, follow through on C only.</p>	



Question 7 : June 06 Q1

Question number	Scheme	Marks
	$\frac{6x^3}{3} + 2x + \frac{x^{\frac{1}{2}}}{\frac{1}{2}} \quad (+c)$ $= 2x^3 + 2x + 2x^{\frac{1}{2}} + c$	M1 A1 A1 B1 4
	<p>M1 for some attempt to integrate $x^n \rightarrow x^{n+1}$</p> <p>1st A1 for either $\frac{6}{3}x^3$ or $\frac{x^{\frac{1}{2}}}{\frac{1}{2}}$ or better</p> <p>2nd A1 for all terms in x correct. Allow $2\sqrt{x}$ and $2x^1$.</p> <p>B1 for $+c$, when first seen with a changed expression.</p>	



Question 8 : June 06 Q10

Question number	Scheme	Marks
(a)	$f(x) = \frac{2x^2}{2} + \frac{3x^{-1}}{-1} (+c)$ $(3, 7\frac{1}{2})$ gives $\frac{15}{2} = 9 - \frac{3}{3} + c$ $c = -\frac{1}{2}$	$-\frac{3}{x}$ is OK 3^2 or 3^{-1} are OK instead of 9 or $\frac{1}{3}$ M1A1 M1A1 f.t. A1 (5)
(b)	$f(-2) = 4 + \frac{3}{2} - \frac{1}{2} \quad (*)$	B1c.s.o. (1)
(c)	$m = -4 + \frac{3}{4}, = -3.25$ Equation of tangent is: $y - 5 = -3.25(x + 2)$ $4y + 13x + 6 = 0$	M1, A1 M1 A1 (4) o.e.
10		
(a)	1 st M1 for some attempt to integrate $x^n \rightarrow x^{n+1}$ 1 st A1 for both x terms as printed or better. Ignore $(+c)$ here. 2 nd M1 for use of $(3, 7\frac{1}{2})$ or $(-2, 5)$ to form an equation for c . There must be some correct substitution. No $+c$ is M0. Some changes in x terms of function needed. 2 nd A1 f.t. for a correct equation for c . Follow through their integration. They must tidy up fraction/fraction and signs (e.g. - - to +).	
(b)	B1cso If $(-2, 5)$ is used to find c in (a) B0 here unless they verify $f(3)=7.5$.	
(c)	1 st M1 for attempting $m = f'(\pm 2)$ 1 st A1 for $-\frac{13}{4}$ or -3.25 2 nd M1 for attempting equation of tangent at $(-2, 5)$, f.t. their m , based on $\frac{dy}{dx}$. 2 nd A1 o.e. must have a, b and c integers and $= 0$.	
Treat (a) and (b) together as a batch of 6 marks.		



Question 9 : Jan 07 Q6

Question number	Scheme	Marks
	<p>(a) $(4 + 3\sqrt{x})(4 + 3\sqrt{x})$ seen, or a numerical value of k seen, ($k \neq 0$). (The k value need not be explicitly stated... see below). $16 + 24\sqrt{x} + 9x$, or $k = 24$</p> <p>(b) $16 \rightarrow cx$ or $kx^{1/2} \rightarrow cx^{3/2}$ or $9x \rightarrow cx^2$ $\int (16 + 24\sqrt{x} + 9x) dx = 16x + \frac{9x^2}{2} + C, +16x^{3/2}$</p>	<p>M1 A1cso (2)</p> <p>M1 A1, A1ft (3)</p> <p>5</p>
	<p>(a) e.g. $(4 + 3\sqrt{x})(4 + 3\sqrt{x})$ alone scores M1 A0, (but <u>not</u> $(4 + 3\sqrt{x})^2$ alone). e.g $16 + 12\sqrt{x} + 9x$ scores M1 A0. $k = 24$ or $16 + 24\sqrt{x} + 9x$, with no further evidence, scores full marks M1 A1. Correct solution only (cso): any wrong working seen loses the A mark.</p> <p>(b) A1: $16x + \frac{9x^2}{2} + C$. Allow 4.5 or $4\frac{1}{2}$ as equivalent to $\frac{9}{2}$. A1ft: $\frac{2k}{3}x^{3/2}$ (candidate's value of k, or general k). For this final mark, allow for example $\frac{48}{3}$ as equivalent to 16, but do <u>not</u> allow unsimplified "double fractions" such as $\frac{24}{(3/2)}$, and do <u>not</u> allow unsimplified "products" such as $\frac{2}{3} \times 24$. A single term is required, e.g. $8x^{3/2} + 8x^{3/2}$ is not enough. An otherwise correct solution with, say, C missing, followed by an incorrect solution including $+ C$ can be awarded full marks (isw, but allowing the C to appear at any stage).</p>	

Question 10 : Jan 07 Q7

Question number	Scheme	Marks
	<p>(a) $3x^2 \rightarrow cx^3$ or $-6 \rightarrow cx$ or $-8x^{-2} \rightarrow cx^{-1}$</p> <p>$f(x) = \frac{3x^3}{3} - 6x - \frac{8x^{-1}}{-1} \quad (+C) \quad \left(x^3 - 6x + \frac{8}{x} \right)$</p> <p>Substitute $x = 2$ <u>and</u> $y = 1$ into a 'changed function' to form an equation in C.</p> <p>$1 = 8 - 12 + 4 + C \quad C = 1$</p> <p>(b) $3 \times 2^2 - 6 - \frac{8}{2^2}$</p> <p>$= 4$</p> <p>Eqn. of tangent: $y - 1 = 4(x - 2)$</p> <p>$y = 4x - 7 \quad (\text{Must be in this form})$</p>	<p>M1</p> <p>A1 A1</p> <p>M1</p> <p>A1cso (5)</p> <p>M1</p> <p>A1</p> <p>M1</p> <p>A1 (4)</p> <p>9</p>
	<p>(a) First 2 A marks: + C is not required, and coefficients need <u>not</u> be simplified, but powers must be simplified.</p> <p>All 3 terms correct: A1 A1</p> <p>Two terms correct: A1 A0</p> <p>Only one term correct: A0 A0</p> <p>Allow the M1 A1 for finding C to be scored either in part (a) or in part (b).</p> <p>(b) 1st M: Substituting $x = 2$ into $3x^2 - 6 - \frac{8}{x^2}$ (must be this function).</p> <p>2nd M: Awarded generously for attempting the equation of a straight line through (2, 1) or (1, 2) with any value of m, however found.</p> <p>2nd M: Alternative is to use (2, 1) or (1, 2) in $y = mx + c$ to <u>find a value</u> for c.</p> <p>If calculation for the gradient value is seen in part (a), it must be <u>used</u> in part (b) to score the first M1 A1 in (b).</p> <p><u>Using (1, 2) instead of (2, 1):</u> Loses the 2nd method mark in (a). Gains the 2nd method mark in (b).</p>	


Question 11 : June 07 Q3

Question number	Scheme	Marks
(c) $x^3 + \frac{8}{3}x^{\frac{3}{2}} + C$	A1: $\frac{3}{3} x^3$ or $\frac{4x^{\frac{3}{2}}}{\left(\frac{3}{2}\right)}$ A1: both, simplified and + C	M1 A1 A1 (3)

(c)	<p>M1 for some attempt to integrate: $x^n \rightarrow x^{n+1}$. Condone misreading $\frac{dy}{dx}$ or $\frac{d^2y}{dx^2}$ for y. (+C alone is not sufficient)</p> <p>1st A1 for either $\frac{3}{3} x^3$ or $\frac{4x^{\frac{3}{2}}}{\left(\frac{3}{2}\right)}$ (or better) $\frac{2}{3} \times 4x^{\frac{3}{2}}$ is OK here too but not for 2nd A1.</p> <p>2nd A1 for <u>both</u> x^3 and $\frac{8}{3}x^{\frac{3}{2}}$ or $\frac{8}{3}x\sqrt{x}$ i.e. simplified terms <u>and</u> +C all on one line. $2\frac{2}{3}$ instead of $\frac{8}{3}$ is OK</p>
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Question 12 : June 07 Q9

Question number	Scheme	Marks
	<p>(a) $f(x) = \frac{6x^3}{3} - \frac{10x^2}{2} - 12x (+C)$</p> <p>$x = 5: \quad 250 - 125 - 60 + C = 65 \quad C = 0$</p> <p>(b) $x(2x^2 - 5x - 12)$ or $(2x^2 + 3x)(x - 4)$ or $(2x + 3)(x^2 - 4x)$</p> <p>$= x(2x + 3)(x - 4)$ (*)</p> <p>(c) </p> <p style="text-align: right;">Shape Through origin $\left(-\frac{3}{2}, 0\right)$ and $(4, 0)$</p>	<p>M1 A1</p> <p>M1 A1 (4)</p> <p>M1</p> <p>A1cso (2)</p> <p>B1</p> <p>B1</p> <p>B1 (3)</p> <p style="text-align: right;">9</p>
(a)	<p>1st M1 for attempting to integrate, $x^n \rightarrow x^{n+1}$</p> <p>1st A1 for all x terms correct, need not be simplified. Ignore $+C$ here.</p> <p>2nd M1 for some use of $x = 5$ and $f(5)=65$ to form an equation in C based on their integration.</p> <p>There must be some visible attempt to use $x = 5$ and $f(5)=65$. No $+C$ is M0.</p> <p>2nd A1 for $C = 0$. This mark cannot be scored unless a suitable equation is seen.</p>	
(b)	<p>M1 for attempting to take out a correct factor or to verify. Allow usual errors on signs.</p> <p>They must get to the equivalent of one of the given partially factorised expressions or, if verifying, $x(2x^2 + 3x - 8x - 12)$ i.e. with no errors in signs.</p> <p>A1cso for proceeding to printed answer with no incorrect working seen. Comment <u>not</u> required.</p> <p>This mark is <u>dependent upon a fully correct solution to part (a)</u> so M1A1M0A0M1A0 for (a) & (b).</p> <p>Will be common or M1A1M1A0M1A0. To score 2 in (b) they must score 4 in (a).</p>	
(c)	<p>1st B1 for positive x^3 shaped curve (with a max and a min) positioned anywhere.</p> <p>2nd B1 for any curve that passes through the origin (B0 if it only touches at the origin)</p> <p>3rd B1 for the two points <u>clearly</u> given as coords or values marked in appropriate places on x axis.</p> <p>Ignore any extra crossing points (they should have lost first B1).</p> <p>Condone $(1.5, 0)$ if clearly marked on $-ve$ x-axis. Condone $(0, 4)$ etc if marked on $+ve$ x axis.</p> <p>Curve can <u>stop</u> (i.e. not pass through) at $(-1.5, 0)$ and $(4, 0)$.</p> <p>A point on the graph overrides coordinates given elsewhere.</p>	



Question 13: Jan 08 Q1

Question number	Scheme	Marks
	$3x^2 \rightarrow kx^3$ or $4x^5 \rightarrow kx^6$ or $-7 \rightarrow kx$ (k a non-zero constant) $\frac{3x^3}{3}$ or $\frac{4x^6}{6}$ (Either of these, simplified or unsimplified) $x^3 + \frac{2x^6}{3} - 7x$ or equivalent unsimplified, such as $\frac{3x^3}{3} + \frac{4x^6}{6} - 7x^1$ $+ C$ (or any other constant, e.g. $+ K$)	M1 A1 A1 B1 (4) 4
	<p>M: Given for increasing by one the power of x in one of the three terms.</p> <p>A marks: 'Ignore subsequent working' after a correct unsimplified version of a term is seen.</p> <p>B: Allow the mark (independently) for an integration constant appearing at any stage (even if it appears, then disappears from the final answer).</p> <p>This B mark can be allowed even when no other marks are scored.</p>	

Question 14 : Jan 08 Q9

Question number	Scheme	Marks
	<p>(a) $4x \rightarrow kx^2$ or $6\sqrt{x} \rightarrow kx^{\frac{3}{2}}$ or $\frac{8}{x^2} \rightarrow kx^{-1}$ (k a non-zero constant)</p> <p>$f(x) = 2x^2, -4x^{\frac{3}{2}}, -8x^{-1}$ (+ C) (+ C not required)</p> <p>At $x = 4, y = 1$: $1 = (2 \times 16) - (4 \times 4^{\frac{3}{2}}) - (8 \times 4^{-1}) + C$ <u>Must be in part (a)</u></p> <p>$C = 3$</p>	<p>M1</p> <p>A1, A1, A1</p> <p>M1</p> <p>A1 (6)</p>
	<p>(b) $f'(4) = 16 - (6 \times 2) + \frac{8}{16} = \frac{9}{2} (= m)$ [M: Attempt $f'(4)$ with the <u>given</u> f'. Must be in part (b)]</p> <p>Gradient of normal is $-\frac{2}{9} (= -\frac{1}{m})$ [M: Attempt perp. grad. rule. Dependent on the use of their $f'(x)$]</p> <p>Eqn. of normal: $y - 1 = -\frac{2}{9}(x - 4)$ (or any equiv. form, e.g. $\frac{y-1}{x-4} = -\frac{2}{9}$)</p> <p>Typical answers for A1: $(y = -\frac{2}{9}x + \frac{17}{9}) (2x + 9y - 17 = 0) (y = -0.2\dot{x} + 1.\dot{8})$</p> <p>Final answer: gradient $-\frac{1}{(\frac{9}{2})}$ or $-\frac{1}{4.5}$ is A0 (but all M marks are available).</p>	<p>M1</p> <p>M1</p> <p>M1 A1 (4)</p>
		10

<p>(a) The first 3 A marks are awarded in the order shown, and the terms must be simplified.</p> <p>'Simplified' coefficient means $\frac{a}{b}$ where a and b are integers with no common factors. Only a single + or - sign is allowed (e.g. $+-$ must be replaced by $-$).</p> <p>2nd M: Using $x = 4$ <u>and</u> $y = 1$ (<u>not</u> $y = 0$) to form an eqn in C. (No C is M0)</p> <p>(b) 2nd M: Dependent upon use of their $f'(x)$.</p> <p>3rd M: eqn. of a straight line through $(4, 1)$ with any gradient except 0 or ∞.</p> <p>Alternative for 3rd M: Using $(4, 1)$ in $y = mx + c$ to <u>find a value</u> of c, but an equation (general or specific) must be seen.</p> <p>Having coords the <u>wrong way round</u>, e.g. $y - 4 = -\frac{2}{9}(x - 1)$, loses the 3rd M mark <u>unless</u> a correct general formula is seen, e.g. $y - y_1 = m(x - x_1)$.</p> <p>N.B. The A mark is scored for <u>any</u> form of the correct equation... be prepared to apply isw if necessary.</p>	
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Question 15 : June 08 Q1

Question Number	Scheme	Marks
	$2x + \frac{5}{3}x^3 + c$	M1 A1 A1 (3) (3 marks)

Question 16 : June 08 Q11

Question Number	Scheme	Marks
(a)	$(x^2 + 3)^2 = x^4 + 3x^2 + 3x^2 + 3^2$ $\frac{(x^2 + 3)^2}{x^2} = \frac{x^4 + 6x^2 + 9}{x^2} = x^2 + 6 + 9x^{-2} \quad (*)$	M1 A1 cso (2)
(b)	$y = \frac{x^3}{3} + 6x + \frac{9}{-1}x^{-1} (+c)$ $20 = \frac{27}{3} + 6 \times 3 - \frac{9}{3} + c$ $c = -4$ $[y =] \frac{x^3}{3} + 6x - 9x^{-1} - 4$	M1 A1 A1 M1 A1 A1 ft (6) (8 marks)



Question 17 : Jan 09 Q2

Question Number	Scheme	Marks
	$(I =) \frac{12}{6}x^6 - \frac{8}{4}x^4 + 3x + c$ $= 2x^6 - 2x^4 + 3x + c$	<p>M1</p> <p>A1A1A1</p> <p>[4]</p>
	<p>M1 for an attempt to integrate $x^n \rightarrow x^{n+1}$ (i.e. ax^6 or ax^4 or ax, where a is any non-zero constant). Also, this M mark can be scored for just the $+c$ (seen at some stage), even if no other terms are correct.</p> <p>1st A1 for $2x^6$ 2nd A1 for $-2x^4$ 3rd A1 for $3x + c$ (or $3x + k$, etc., any appropriate letter can be used as the constant)</p> <p>Allow $3x^1 + c$, but <u>not</u> $\frac{3x^1}{1} + c$.</p> <p>Note that the A marks can be awarded at separate stages, e.g.</p> <p>$\frac{12}{6}x^6 - 2x^4 + 3x$ scores 2nd A1 $\frac{12}{6}x^6 - 2x^4 + 3x + c$ scores 3rd A1 $2x^6 - 2x^4 + 3x$ scores 1st A1 (even though the c has now been lost).</p> <p>Remember that all the A marks are dependent on the M mark.</p> <p>If applicable, isw (ignore subsequent working) after a correct answer is seen.</p> <p>Ignore wrong notation if the intention is clear, e.g. Answer $\int 2x^6 - 2x^4 + 3x + c \, dx$.</p>	

Question 18 : Jan 09 Q4

Question Number	Scheme	Marks
	$(f(x) = \frac{3x^3}{3} - \frac{3x^{\frac{3}{2}}}{\frac{3}{2}} - 7x(+c)$ $= x^3 - 2x^{\frac{3}{2}} - 7x (+c)$ $f(4) = 22 \Rightarrow 22 = 64 - 16 - 28 + c$ $c = 2$	M1 A1A1 M1 A1cso (5) [5]
	<p>1st M1 for an attempt to integrate (x^3 or $x^{\frac{3}{2}}$ seen). The x term is insufficient for this mark and similarly the $+c$ is insufficient.</p> <p>1st A1 for $\frac{3}{3}x^3$ or $-\frac{3x^{\frac{3}{2}}}{\frac{3}{2}}$ (An unsimplified or simplified correct form)</p> <p>2nd A1 for all three x terms correct and simplified... (the simplification may be seen later). The $+c$ is not required for this mark.</p> <p>Allow $-7x^1$, but <u>not</u> $-\frac{7x^1}{1}$.</p> <p>2nd M1 for an attempt to use $x = 4$ <u>and</u> $y = 22$ in a changed function (even if differentiated) to form an equation in c.</p> <p>3rd A1 for $c = 2$ with no earlier incorrect work (a final expression for $f(x)$ is not required).</p>	



Question 19 : June 09 Q3

Question Number	Scheme	Marks
	$\frac{2x^4}{4} + \frac{3x^{-1}}{-1} (+C)$ $\frac{x^4}{2} - 3x^{-1} + C$	M1 A1 A1 (3)

<p>M1 for some attempt to integrate an x term of the given y. $x^n \rightarrow x^{n+1}$</p> <p>1st A1 for both x terms correct but unsimplified- as printed or better. Ignore $+c$ here</p> <p>2nd A1 for both x terms correct and simplified and $+c$. Accept $-\frac{3}{x}$ but <u>NOT</u> $+ -3x^{-1}$</p> <p>Condone the $+c$ appearing on the first (unsimplified) line but missing on the final (simplified) line</p> <p>Apply ISW if a correct answer is seen</p> <p>If part (b) is attempted first and this is clearly labelled then apply the scheme and allow the marks. Otherwise assume the first solution is for part (a).</p>	
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Question 20 : Jan 10 Q4

Question number	Scheme	Marks
	$x\sqrt{x} = x^{\frac{3}{2}}$ (Seen, or implied by correct integration) $x^{-\frac{1}{2}} \rightarrow kx^{\frac{1}{2}}$ or $x^{\frac{3}{2}} \rightarrow kx^{\frac{5}{2}}$ (k a non-zero constant) $(y =) \frac{5x^{\frac{1}{2}}}{\frac{1}{2}} \dots + \frac{x^{\frac{5}{2}}}{\frac{5}{2}} (+C)$ ("y =" and "+C" are not required for these marks) $35 = \frac{5 \times 4^{\frac{1}{2}}}{\frac{1}{2}} + \frac{4^{\frac{5}{2}}}{\frac{5}{2}} + C$ An equation in C is required (see conditions below). (With their terms simplified or unsimplified). $C = \frac{11}{5}$ or equivalent $2\frac{1}{5}, 2.2$ $y = 10x^{\frac{1}{2}} + \frac{2x^{\frac{5}{2}}}{5} + \frac{11}{5}$ (Or equivalent <u>simplified</u>) I.s.w. if necessary, e.g. $y = 10x^{\frac{1}{2}} + \frac{2x^{\frac{5}{2}}}{5} + \frac{11}{5} = 50x^{\frac{1}{2}} + 2x^{\frac{5}{2}} + 11$ The final A mark requires an <u>equation</u> "y = ..." with correct x terms (see below).	B1 M1 A1... A1 M1 A1 A1 ft [7]
	B mark: $x^{\frac{3}{2}}$ often appears from integration of \sqrt{x} , which is B0. 1 st A: Any unsimplified or simplified correct form, e.g. $\frac{5\sqrt{x}}{0.5}$. 2 nd A: Any unsimplified or simplified correct form, e.g. $\frac{x^2\sqrt{x}}{2.5}, \frac{2(\sqrt{x})^5}{5}$. 2 nd M: Attempting to use $x = 4$ and $y = 35$ in a changed function (even if differentiated) to form an equation in C . 3 rd A: Obtaining $C = \frac{11}{5}$ with no earlier incorrect work. 4 th A: Follow-through <u>only</u> the value of C (i.e. the other terms must be correct). Accept equivalent <u>simplified</u> terms such as $10\sqrt{x} + 0.4x^2\sqrt{x} \dots$	



Question 21 : June 10 Q2

Question Number	Scheme	Marks
	$\frac{8x^4}{4} + \frac{6x^{\frac{3}{2}}}{\frac{3}{2}} - 5x + c$ $= 2x^4 + 4x^{\frac{3}{2}} - 5x + c$	<p>M1 A1</p> <p>A1 A1</p> <p>4</p>
	Notes	
	<p>M1 for some attempt to integrate a term in x: $x^n \rightarrow x^{n+1}$</p> <p>1st A1 for correct, possibly un-simplified x^4 or $x^{\frac{3}{2}}$ term. e.g. $\frac{8x^4}{4}$ or $\frac{6x^{\frac{3}{2}}}{\frac{3}{2}}$</p> <p>2nd A1 for <u>both</u> $2x^4$ and $4x^{\frac{3}{2}}$ terms correct and simplified on the same line N.B. some candidates write $4\sqrt{x^3}$ or $4x^{1\frac{1}{2}}$ which are, of course, fine for A1</p> <p>3rd A1 for $-5x + c$. Accept $-5x^1 + c$. The $+c$ must appear on the same line as the $-5x$ N.B. We do not need to see one line with a fully correct integral</p> <p>Ignore ISW (ignore incorrect subsequent working) if a correct answer is followed by an incorrect version.</p> <p>Condone poor use of notation e.g. $\int 2x^4 + 4x^{\frac{3}{2}} - 5x + c$ will score full marks.</p>	

Question 22 : June 10 Q11

Question Number	Scheme	Marks
(a)	$(y =) \frac{3x^2}{2} - \frac{5x^{\frac{1}{2}}}{\frac{1}{2}} - 2x \quad (+c)$ $f(4) = 5 \Rightarrow 5 = \frac{3}{2} \times 16 - 10 \times 2 - 8 + c$ $\underline{c = 9}$ $\left[f(x) = \frac{3}{2}x^2 - 10x^{\frac{1}{2}} - 2x + 9 \right]$	M1A1A1 M1 A1 (5)
(b)	$m = 3 \times 4 - \frac{5}{2} - 2 \quad \left(= 7.5 \text{ or } \frac{15}{2} \right)$ <p>Equation is: $y - 5 = \frac{15}{2}(x - 4)$</p> $\underline{2y - 15x + 50 = 0} \quad \text{o.e.}$	M1 M1A1 A1 (4) (9marks)
(a)	1 st M1 for an attempt to integrate $x^n \rightarrow x^{n+1}$ 1 st A1 for at least 2 correct terms in x (unsimplified) 2 nd A1 for all 3 terms in x correct (condone missing $+c$ at this point). Needn't be simplified 2 nd M1 for using the point (4, 5) to form a linear equation for c . Must use $x = 4$ and $y = 5$ and have no x term and the function must have "changed". 3 rd A1 for $c = 9$. The final expression is not required.	
(b)	1 st M1 for an attempt to evaluate $f'(4)$. Some correct use of $x = 4$ in $f'(x)$ but condone slips. They must therefore have at least 3×4 or $-\frac{5}{2}$ and clearly be using $f'(x)$ with $x = 4$. Award this mark wherever it is seen. 2 nd M1 for using their value of m [or their $-\frac{1}{m}$] (provided it clearly comes from using $x = 4$ in $f(x)$) to form an equation of the line through (4,5)). <p>Allow this mark for an attempt at a normal or tangent. Their m must be numerical. Use of $y = mx + c$ scores this mark when c is found.</p> 1 st A1 for any correct expression for the equation of the line 2 nd A1 for any correct equation with integer coefficients. An "=" is required. e.g. $2y = 15x - 50$ etc as long as the equation is correct and has integer coefficients.	
Normal	Attempt at normal can score both M marks in (b) but A0A0	



Question 23 : Jan 11 Q2

Question Number	Scheme	Marks
	$\left(\int =\right) \frac{12x^6}{6}, -\frac{3x^3}{3}, +\frac{4x^{\frac{4}{3}}}{\frac{4}{3}}, (+c)$ $= \underline{2x^6 - x^3 + 3x^{\frac{4}{3}} + c}$	M1A1,A1,A1 A1 5
	Notes	
	<p>M1 for some attempt to integrate: $x^n \rightarrow x^{n+1}$ i.e ax^6 or ax^3 or $ax^{\frac{4}{3}}$ or $ax^{\frac{1}{3}}$, where a is a non zero constant</p> <p>1st A1 for $\frac{12x^6}{6}$ or better</p> <p>2nd A1 for $-\frac{3x^3}{3}$ or better</p> <p>3rd A1 for $\frac{4x^{\frac{4}{3}}}{\frac{4}{3}}$ or better</p> <p>4th A1 for each term correct and simplified and the $+c$ occurring in the final answer</p>	



Question 25 : June 11 02

	Notes
(b)	<p>1st M: Attempt to integrate $x^n \rightarrow x^{n+1}$ (for either term)</p> <p>1st A: ft their p and q, but terms need not be simplified (+C not required for this mark)</p> <p>2nd M: Using $x = 4$ <u>and</u> $y = 90$ to form an equation in C.</p> <p>2nd A: cao</p> <p>3rd A: answer as shown with simplified correct coefficients and powers – but follow through their value for C</p> <p>If there is a 'restart' in part (b) it can be marked independently of part (a), but marks for part (a) cannot be scored for work seen in (b).</p> <p><u>Numerator and denominator integrated separately:</u></p> <p>First M mark cannot be awarded so only mark available is second M mark. So 1 out of 5 marks.</p>



Question 26 : June 11 Q6

Question Number	Scheme	Marks
(a)	$\frac{dy}{dx} = 10x^4 - 3x^{-4}$ or $10x^4 - \frac{3}{x^4}$	M1 A1 A1 (3)
(b)	$(\int =) \frac{2x^6}{6} + 7x + \frac{x^{-2}}{-2} = \frac{x^6}{3} + 7x - \frac{x^{-2}}{2} + C$	M1 A1 A1 B1 (4) 7
<p style="text-align: center;">Notes</p> <p>(a) M1: Attempt to differentiate $x^n \rightarrow x^{n-1}$ (for any of the 3 terms) i.e. ax^4 or ax^{-4}, where a is any non-zero constant or the 7 differentiated to give 0 is sufficient evidence for M1 1st A1: One correct (non-zero) term, possibly unsimplified. 2nd A1: Fully correct simplified answer.</p> <p>(b) M1: Attempt to integrate $x^n \rightarrow x^{n+1}$ (i.e. ax^6 or ax or ax^{-2}, where a is any non-zero constant). 1st A1: Two correct terms, possibly unsimplified. 2nd A1: All three terms correct and simplified. Allow correct equivalents to printed answer, e.g. $\frac{x^6}{3} + 7x - \frac{1}{2x^2}$ or $\frac{1}{3}x^6 + 7x - \frac{1}{2}x^{-2}$ Allow $\frac{1x^6}{3}$ or $7x^1$ B1: $+ C$ appearing at any stage in part (b) (independent of previous work)</p>		