## Statistical Distribution : Probability Distribution - Edexcel Past Exam Questions

1. The random variable $X$ has probability function

$$
\begin{equation*}
\mathrm{P}(X=x)=k x, \quad x=1,2, \ldots, 5 . \tag{2}
\end{equation*}
$$

(a) Show that $k=\frac{1}{15}$.

Find
(b) $\mathrm{P}(X<4)$,

Jan 05 Q4(edited)
2. The random variable $X$ has probability function

$$
\mathrm{P}(X=x)= \begin{cases}k x, & x=1,2,3, \\ k(x+1), & x=4,5,\end{cases}
$$

where $k$ is a constant.
(a) Find the value of $k$.
3. The random variable $X$ has probability function

$$
\mathrm{P}(X=x)=\frac{(2 x-1)}{36} \quad x=1,2,3,4,5,6 .
$$

(a) Construct a table giving the probability distribution of $X$.

Find
(b) $\mathrm{P}(2<X \leq 5)$
4. The random variable $X$ has probability distribution

| $x$ | 1 | 3 | 5 | 7 | 9 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{P}(X=x)$ | 0.2 | 0.3 | 0.2 | $q$ | 0.15 |

Find
(a) the value of $q$,
(b) $\mathrm{P}(4<X \leq 7)$.

## June 07 Q7(edited)

5. Tetrahedral dice have four faces. Two fair tetrahedral dice, one red and one blue, have faces numbered $0,1,2$, and 3 respectively. The dice are rolled and the numbers face down on the two dice are recorded. The random variable $R$ is the score on the red die and the random variable $B$ is the score on the blue die.
(a) Find $\mathrm{P}(R=3$ and $B=0)$.

The random variable $T$ is $R$ multiplied by $B$.
(b) Complete the diagram below to represent the sample space that shows all the possible values of $T$.

| 3 |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| 2 |  | 2 |  |  |
| 1 | 0 |  |  |  |
| 0 |  |  |  |  |
|  | 0 | 1 | 2 | 3 |

Sample space diagram of $T$
6. The discrete random variable $X$ has probability function

$$
\mathrm{P}(X=x)=\left\{\begin{array}{cl}
a(3-x) & x=0,1,2 \\
b & x=3
\end{array}\right.
$$

(a) Find $\mathrm{P}(X=2)$ and copy and complete the table below.

| $x$ | 0 | 1 | 2 | 3 |
| :---: | :---: | :---: | :---: | :---: |
| $\mathrm{P}(X=x)$ | $3 a$ | $2 a$ |  | $b$ |

Given that $\mathrm{b}=0.4$
(b) find the value of $a$

Find
(c) $\mathrm{P}(0.5<X<3)$,
7. The probability function of a discrete random variable $X$ is given by

$$
\mathrm{p}(x)=k x^{2}, \quad x=1,2,3 .
$$

where $k$ is a positive constant.
(a) Show that $k=\frac{1}{14}$.

Find
(b) $\mathrm{P}(X \geq 2)$,
8. The discrete random variable $X$ has probability distribution given by

| $x$ | -1 | 0 | 1 | 2 | 3 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{P}(X=x)$ | $\frac{1}{5}$ | $a$ | $\frac{1}{10}$ | $a$ | $\frac{1}{5}$ |

where $a$ is a constant.
(a) Find the value of $a$.

The random variable $Y=6-2 X$.
(b) Calculate $\mathrm{P}(X \geq Y)$.
9. The discrete random variable $X$ has the probability distribution

| $x$ | 1 | 2 | 3 | 4 |
| :---: | :---: | :---: | :---: | :---: |
| $\mathrm{P}(X=x)$ | $k$ | $2 k$ | $3 k$ | $4 k$ |

(a) Show that $k=0.1$

Two independent observations $X_{1}$ and $X_{2}$ are made of $X$.
(b) Show that $\mathrm{P}\left(X_{1}+X_{2}=4\right)=0.1$
(c) Complete the probability distribution table for $X_{1}+X_{2}$.

| $y$ | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{P}\left(X_{1}+X_{2}=y\right)$ | 0.01 | 0.04 | 0.10 |  | 0.25 | 0.24 |  |

(d) Find $\mathrm{P}\left(1.5<X_{1}+X_{2} \leq 3.5\right)$
10. The discrete random variable $Y$ has the probability distribution

| $y$ | 1 | 2 | 3 | 4 |
| :---: | :---: | :---: | :---: | :---: |
| $\mathrm{P}(Y=y)$ | 0.1 | 0.4 | 0.3 | c |

where $c$ is a constant.
(a) Find the value of $c$.
(b) Find $\mathrm{P}(3 Y+2 \geq 8)$.
11. A spinner is designed so that the score $S$ is given by the following probability distribution.

| $s$ | 0 | 1 | 2 | 4 | 5 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{P}(S=s)$ | $p$ | 0.25 | 0.25 | 0.20 | 0.20 |

(a) Find the value of $p$.

Tom and Jess play a game with this spinner. The spinner is spun repeatedly and $S$ counters are awarded on the outcome of each spin. If $S$ is even then Tom receives the counters and if $S$ is odd then Jess receives them. The first player to collect 10 or more counters is the winner.
(b) Find the probability that Jess wins after 2 spins.
(c) Find the probability that Tom wins after exactly 3 spins.
(d) Find the probability that Jess wins after exactly 3 spins.

