## Circles - Edexcel Past Exam Questions

1. The circle $C$, with centre at the point $A$, has equation $x^{2}+y^{2}-10 x+9=0$.

Find
(a) the coordinates of $A$,
(b) the radius of $C$,
(c) the coordinates of the points at which $C$ crosses the $x$-axis.

Given that the line $l$ with gradient $\frac{7}{2}$ is a tangent to $C$, and that $l$ touches $C$ at the point $T$,
(d) find an equation of the line which passes through $A$ and $T$.

June 05 Q8
2. The points $A$ and $B$ have coordinates $(5,-1)$ and $(13,11)$ respectively.
(a) Find the coordinates of the mid-point of $A B$.

Given that $A B$ is a diameter of the circle $C$,
(b) find an equation for $C$.
3.

Figure 1


In Figure $1, A(4,0)$ and $B(3,5)$ are the end points of a diameter of the circle $C$.
Find
(a) the exact length of $A B$,
(b) the coordinates of the midpoint $P$ of $A B$,
(c) an equation for the circle $C$.
4.

Figure 1


The line $y=3 x-4$ is a tangent to the circle $C$, touching $C$ at the point $\mathrm{P}(2,2)$, as shown in Figure 1 . The point $Q$ is the centre of $C$.
(a) Find an equation of the straight line through $P$ and $Q$.

Given that $Q$ lies on the line $y=1$,
(b) show that the $x$-coordinate of $Q$ is 5 ,
(c) find an equation for $C$.

## June 06 Q7

5. The line joining points $(-1,4)$ and $(3,6)$ is a diameter of the circle $C$.

Find an equation for $C$.
Jan 07 Q3
6.


Figure 3
The points $A$ and $B$ lie on a circle with centre $P$, as shown in Figure 3.
The point $A$ has coordinates $(1,-2)$ and the mid-point $M$ of $A B$ has coordinates $(3,1)$. The line $l$ passes through the points $M$ and $P$.
(a) Find an equation for $l$.

Given that the $x$-coordinate of $P$ is 6 ,
(b) use your answer to part (a) to show that the $y$-coordinate of $P$ is -1 ,
(c) find an equation for the circle.
7. The circle $C$ has centre $(3,1)$ and passes through the point $P(8,3)$.
(a) Find an equation for $C$.
(b) Find an equation for the tangent to $C$ at $P$, giving your answer in the form $a x+b y+c=0$, where $a, b$ and $c$ are integers.
8.


The points $P(-3,2), Q(9,10)$ and $R(a, 4)$ lie on the circle $C$, as shown in Figure 2.
Given that $P R$ is a diameter of $C$,
(a) show that $a=13$,
(b) find an equation for $C$.
9. The circle $C$ has equation

$$
x^{2}+y^{2}-6 x+4 y=12
$$

(a) Find the centre and the radius of $C$.

The point $P(-1,1)$ and the point $Q(7,-5)$ both lie on $C$.
(b) Show that $P Q$ is a diameter of $C$.

The point $R$ lies on the positive $y$-axis and the angle $P R Q=90^{\circ}$.
(c) Find the coordinates of $R$.
10.


Figure 3
Figure 3 shows a sketch of the circle $C$ with centre $N$ and equation

$$
(x-2)^{2}+(y+1)^{2}=\frac{169}{4}
$$

(a) Write down the coordinates of $N$.
(b) Find the radius of $C$.

The chord $A B$ of $C$ is parallel to the $x$-axis, lies below the $x$-axis and is of length 12 units as shown in Figure 3.
(c) Find the coordinates of $A$ and the coordinates of $B$.
(d) Show that angle $A N B=134.8^{\circ}$, to the nearest 0.1 of a degree.

The tangents to $C$ at the points $A$ and $B$ meet at the point $P$.
(e) Find the length $A P$, giving your answer to 3 significant figures
11. The circle $C$ has centre $A(2,1)$ and passes through the point $B(10,7)$.
(a) Find an equation for $C$.

The line $l_{1}$ is the tangent to $C$ at the point $B$.
(b) Find an equation for $l_{1}$.

The line $l_{2}$ is parallel to $l_{1}$ and passes through the mid-point of $A B$.

Given that $l_{2}$ intersects $C$ at the points $P$ and $Q$,
(c) find the length of $P Q$, giving your answer in its simplest surd form.

June 10 Q10
12. The points $A$ and $B$ have coordinates $(-2,11)$ and $(8,1)$ respectively.

Given that $A B$ is a diameter of the circle $C$,
(a) show that the centre of $C$ has coordinates $(3,6)$,
(b) find an equation for $C$.
(c) Verify that the point $(10,7)$ lies on $C$.
(d) Find an equation of the tangent to $C$ at the point (10, 7), giving your answer in the form $y=m x+c$, where $m$ and $c$ are constants.

Jan 11 Q9
13. The circle $C$ has equation

$$
x^{2}+y^{2}+4 x-2 y-11=0 .
$$

Find
(a) the coordinates of the centre of $C$,
(b) the radius of $C$,
(c) the coordinates of the points where $C$ crosses the $y$-axis, giving your answers as simplified surds.

