Algebraic Expression - Edexcel Past Exam Questions MARK SCHEME

Question 1: Jan 05 Q1


## Question 2: June 05 Q1

| Question Number | Scheme |  | Marks |  |
| :---: | :---: | :---: | :---: | :---: |
| (a) |  |  |  | (1) |
| (b) | $\begin{aligned} 8^{-\frac{2}{3}} & =\frac{1}{\sqrt[3]{64}} \text { or } \frac{1}{(a)^{2}} \text { or } \frac{1}{\sqrt[3]{8^{2}}} \text { or } \frac{1}{8^{\frac{2}{3}}} \\ & =\frac{1}{4} \text { or } 0.25 \end{aligned}$ | Allow $\pm$ | M1 A1 | (2) |
| (b) | M1 for understanding that "-" power means reciprocal $8^{\frac{2}{3}}=4$ is M0A0 and $-\frac{1}{4}$ is M1A0 |  |  |  |

Question 3: June 05 Q7

| Question <br> Number | Scheme | Marks |
| :---: | :--- | :--- |
| (a) | $(3-\sqrt{x})^{2}=9-6 \sqrt{x}+x$ <br> $\div b y \sqrt{x} \rightarrow 9 x^{-\frac{1}{2}}-6+x^{\frac{1}{2}}$ | M1 |
| (a) | M1 Attempt to multiply out $(3-\sqrt{x})^{2}$. Must have 3 or 4 terms, allow one sign error <br> A1 cso Fully correct solution to printed answer. Penalise wrong working. |  |

Question 4: Jan 06 Q1

| Question number | Scheme | Marks |
| :---: | :---: | :---: |
|  | $\begin{array}{ll} x\left(x^{2}-4 x+3\right) & \text { Factor of } x . \text { (Allow }(x-0)) \\ =x(x-3)(x-1) & \text { Factorise } 3 \text { term quadratic } \tag{3} \end{array}$ | M1 <br> M1 A1 <br> Total 3 marks |
|  | Alternative: |  |
|  | $\left(x^{2}-3 x\right)(x-1)$ or $\left(x^{2}-x\right)(x-3)$ scores the second M1 (allow $\pm$ for each sign), then $x(x-3)(x-1)$ scores the first M 1 , and A 1 if correct. <br> Alternative: <br> Finding factor $(x-1)$ or $(x-3)$ by the factor theorem scores the second M1, then completing, using factor $x$, scores the first M1, and A1 if correct. <br> Factors "split": e.g. $x\left(x^{2}-4 x+3\right) \Rightarrow(x-3)(x-1)$. Allow full marks. <br> Factor $x$ not seen: e.g. Dividing by $x \Rightarrow(x-3)(x-1)$. M0 M1 A0. <br> If an equation is solved, i.s.w. |  |

Question 5: Jan 06 Q5


Question 6: June 06 Q6

| Question number | Scheme | Marks |
| :---: | :---: | :---: |
| (a) (b) | $\begin{aligned} & 16+4 \sqrt{3}-4 \sqrt{3}-(\sqrt{3})^{2} \text { or } 16-3 \\ & =13 \\ & \frac{26}{4+\sqrt{3}} \times \frac{4-\sqrt{3}}{4-\sqrt{3}} \end{aligned}$ <br> $=\frac{26(4-\sqrt{3})}{13}=\underline{8-2 \sqrt{3}} \quad$ or $\quad 8+(-2) \sqrt{3} \quad$ or $\quad a=8$ and $b=-2$ | M1  <br> Alc.a.o (2) <br> M1  <br>   <br> A1 (2) <br>  4 |
| (a) (b) | M1 For 4 terms, at least 3 correct <br> e.g. $8+4 \sqrt{3}-4 \sqrt{3}-(\sqrt{3})^{2}$ or $16 \pm 8 \sqrt{3}-(\sqrt{3})^{2}$ or $16+3$ <br> $4^{2}$ instead of 16 is OK <br> $(4+\sqrt{3})(4+\sqrt{3})$ scores M0A0 <br> M1 <br> For a correct attempt to rationalise the denominator <br> Can be implied <br> NB $\frac{-4+\sqrt{3}}{-4+\sqrt{3}}$ is OK |  |

Question 7: June 06 Q9

| Question number | Scheme ${ }^{\text {a }}$ Marks |
| :---: | :---: |
| (a) (b) (c) |  |
| (a) (b) (c) | M1 for a correct method to get the factor of $x . \quad x$ ( as printed is the minimum. <br> $1^{\text {st }} \mathrm{A} 1$ for $b=-8$ or $c=15$. <br> -8 comes from -6-2 and must be coefficient of $x$, and 15 from $6 \times 2+3$ and must have no $x$ s. <br> $2^{\text {nd }} \mathrm{Al}$ for $a=1, b=-8$ and $c=15$. Must have $x\left(x^{2}-8 x+15\right)$. <br> M1 for attempt to factorise their $3 T Q$ from part (a). <br> A1 for all 3 terms correct. They must include the $x$. <br> For part (c) they must have at most 2 non-zero roots of their $\mathrm{f}(x)=0$ to ft their 3 and their 5 . <br> $1^{\text {st }}$ B1 for correct shape (i.e. from bottom left to top right and two turning points.) <br> $2^{\text {nd }}$ B1f.t. for crossing at their 3 or their 5 indicated on graph or in text. <br> $3^{\text {rd }}$ B1f.t. if graph passes through $(0,0)$ [needn't be marked] and both their 3 and their 5 . |

Question 8: Jan 07 Q2

| Question | Scheme | Marks |
| :---: | :---: | :---: |
|  | (a) $6 \sqrt{ } 3$ $(a=6)$ <br> (b) Expanding $(2-\sqrt{ } 3)^{2}$ to get 3 or 4 separate terms <br> 7, $-4 \sqrt{ } 3$ $(b=7, c=-4)$ | B1 M1 A1, A1 |
|  | (a) $\pm 6 \sqrt{ } 3$ also scores B1. <br> (b) M1: The 3 or 4 terms may be wrong. <br> $1^{\text {st }} \mathrm{A} 1$ for $7,2^{\text {nd }} \mathrm{A} 1$ for $-4 \sqrt{ } 3$. <br> Correct answer $7-4 \sqrt{ } 3$ with no working scores all 3 marks. $7+4 \sqrt{ } 3$ with or without working scores M1 A1 A0. <br> Other wrong answers with no working score no marks. |  |

## Question 9: June 07 Q1



## Question 10: June 07 Q2

| Question | Scheme | Marks |
| :---: | :---: | :---: |
|  | (a) Attempt $\sqrt[3]{8}$ or $\sqrt[3]{\left(8^{4}\right)}$ $=\underline{16}$ <br> (b) $5 x^{\frac{1}{3}}$ $5, x^{\frac{1}{3}}$ | $\begin{array}{ll}\text { M1 } \\ \text { A1 } \\ \text { B1, B1 } & \\ & \text { (2) } \\ & 4\end{array}$ |
| (a) | M1 for: 2 (on its own) or $\left(2^{3}\right)^{\frac{4}{3}}$ or $\sqrt[3]{8}$ or $(\sqrt[3]{8})^{4}$ or $2^{4}$ or $\sqrt[3]{8^{4}}$ or $\sqrt[3]{4096}$ $8^{3}$ or 512 or $(4096)^{\frac{1}{5}}$ is M0 <br> A1 for 16 only <br> $1^{\text {st }} \mathrm{B} 1$ for 5 on its own or $\times$ something. <br> So e.g. $\frac{5 x^{\frac{4}{3}}}{x}$ is B1 But $5^{\frac{1}{3}}$ is B0 <br> An expression showing cancelling is not sufficient <br> (see first expression of QC0184500123945 the mark is scored for the second expression) <br> $2^{\text {nd }}$ B1 for $x^{\frac{1}{3}}$ <br> Can use ISW (incorrect subsequent working) <br> e.g $5 x^{\frac{4}{3}}$ scores B1B0 but it may lead to $\sqrt[3]{5 x^{4}}$ which we ignore as ISW. <br> Correct answers only score full marks in both parts. |  |
| (b) |  |  |

## Question 11: Jan 08 Q2

| Question | Scheme |  |  |
| :---: | :---: | :---: | :---: |
|  | (a) 2 <br> (b) $x^{9}$ seen, or $(\text { answer to }(\mathrm{a}))^{3}$ seen, or $\left(2 x^{3}\right)^{3}$ seen. $8 x^{9}$ | $\begin{aligned} & \text { B1 } \\ & \text { M1 } \\ & \text { A1 } \end{aligned}$ | (1) (2) |
|  | (b) M: Look for $x^{9}$ first... if seen, this is M1. <br> If not seen, look for (answer to (a) $)^{3}$, e.g. $2^{3} \ldots$ this would score M1 even if it does not subsequently become 8 . (Similarly for other answers to (a)). <br> In $\left(2 x^{3}\right)^{3}$, the $2^{3}$ is implied, so this scores the M mark. <br> Negative answers: <br> (a) Allow -2 . Allow $\pm 2$. Allow ' 2 or -2 '. <br> (b) Allow $\pm 8 x^{9}$. Allow ' $8 x^{9}$ or $-8 x^{9}$. <br> N.B. If part (a) is wrong, it is possible to 'restart' in part (b) and to score full marks in part (b). |  |  |

Question 12: Jan 08 Q3


## Question 13: June 08 Q2

| Question <br> Number | Scheme | Marks |
| :--- | :--- | ---: |
|  | $x\left(x^{2}-9\right)$ or $(x \pm 0)\left(x^{2}-9\right)$ or $(x-3)\left(x^{2}+3 x\right)$ or $(x+3)\left(x^{2}-3 x\right)$ | B1 |
|  | $x(x-3)(x+3)$ | M1 A1 (3) |
| (3 marks) |  |  |

## Question 14: Jan 09 Q1

| Question Number | Scheme | Marks |
| :---: | :---: | :---: |
| (a) <br> (b) | 5 <br> ( $\pm 5$ is B 0 ) | M1 <br> A1 <br> (2) <br> [3] |
| (b) | M1 follow through their value of 5. Must have reciprocal and square. $5^{-2}$ is not sufficient to score this mark, unless $\frac{1}{5^{2}}$ follows this. A negative introduced at any stage can score the M1 but not the A1, e.g. $125^{-2 / 3}=\left(-\frac{1}{5}\right)^{2}=\frac{1}{25} \quad$ scores M1 A0 $125^{-2 / 3}=-\left(\frac{1}{5}\right)^{2}=-\frac{1}{25} \quad \text { scores M1 A0. }$ <br> Correct answer with no working scores both marks. <br> Alternative: $\frac{1}{\sqrt[3]{125^{2}}}$ or $\frac{1}{\left(125^{2}\right)^{1 / 3}}$ M1 (reciprocal and the correct number squared) $\begin{aligned} ( & \left.=\frac{1}{\sqrt[3]{15625}}\right) \\ & =\frac{1}{25} \quad \text { A1 } \end{aligned}$ |  |

Question 15: Jan 09 Q3

| Question Number | Scheme | Marks |
| :---: | :---: | :---: |
|  | $\sqrt{7}^{2}+2 \sqrt{7}-2 \sqrt{7}-2^{2}$, or $7-4$ or an exact equivalent such as $\sqrt{49}-2^{2}$ $=3$ | M1 <br> A1 <br> [2] |
|  | M1 for an expanded expression. At worst, there can be one wrong term and one wrong sign, or two wrong signs. $\begin{aligned} & \text { e.g. } 7+2 \sqrt{7}-2 \sqrt{7}-2 \text { is M1 (one wrong term }-2 \text { ) } \\ & 7+2 \sqrt{7}+2 \sqrt{7}+4 \text { is M1 (two wrong signs }+2 \sqrt{7} \text { and }+4 \text { ) } \\ & 7+2 \sqrt{7}+2 \sqrt{7}+2 \text { is M1 (one wrong term }+2 \text {, one wrong sign }+2 \sqrt{7} \text { ) } \\ & \sqrt{7}+2 \sqrt{7}-2 \sqrt{7}+4 \text { is M1 (one wrong term } \sqrt{7} \text {, one wrong sign + 4) } \\ & \sqrt{7}+2 \sqrt{7}-2 \sqrt{7}-2 \text { is M0 (two wrong terms } \sqrt{7} \text { and }-2 \text { ) } \\ & 7+\sqrt{14}-\sqrt{14}-4 \text { is M0 (two wrong terms } \sqrt{14} \text { and }-\sqrt{14} \text { ) } \end{aligned}$ <br> If only 2 terms are given, they must be correct, i.e. $(7-4)$ or an equivalent unsimplified version to score M1. <br> The terms can be seen separately for the M1. <br> Correct answer with no working scores both marks. |  |

Question 16: Jan 09 Q6

| Question Number | Scheme | Marks |
| :---: | :---: | :---: |
| (a) | $\begin{array}{lll} 2 x^{3 / 2} & \text { or } p=\frac{3}{2} & \text { (Not } 2 x \sqrt{x} \text { ) } \\ -x \text { or }-x^{1} \text { or } q=1 & \tag{2} \end{array}$ | B1 B1 |
| (a) | $\begin{array}{ll} 1^{\text {st }} \mathrm{B} 1 & \text { for } p=1.5 \text { or exact equivalent } \\ 2^{\text {nd }} \mathrm{B} 1 & \text { for } q=1 \end{array}$ |  |

Question 17: June 09 Q1

| Question Number | Scheme | Marks |
| :---: | :---: | :---: |
|  | $\begin{aligned} & (3 \sqrt{7})^{2}=63 \\ & (8+\sqrt{5})(2-\sqrt{5})=16-5+2 \sqrt{ } 5-8 \sqrt{ } 5 \\ & \quad=11,-6 \sqrt{5} \end{aligned}$ | $\begin{aligned} & \text { B1 } \\ & \text { M1 } \\ & \text { A1, A1 } \end{aligned}$ |
|  |  | (3) <br> [4] |
| (a) <br> (b) | B1 for 63 only <br> M1 for an attempt to expand their brackets with $\geq 3$ terms correct. <br> They may collect the $\sqrt{5}$ terms to get $16-5-6 \sqrt{5}$ <br> Allow $-\sqrt{5} \times \sqrt{5}$ or $-(\sqrt{5})^{2}$ or $-\sqrt{25}$ instead of the -5 <br> These 4 values may appear in a list or table but they should have minus signs included <br> The next two marks should be awarded for the final answer but check that correct values follow from correct working. Do not use ISW rule <br> $1^{\text {st }}$ A1 for 11 from $16-5$ or $-6 \sqrt{5}$ from $-8 \sqrt{5}+2 \sqrt{5}$ <br> $2^{\text {nd }}$ A1 for both 11 and $-6 \sqrt{5}$. <br> S.C - Double sign error in expansion <br> For $16-5-2 \sqrt{5}+8 \sqrt{5}$ leading to $11+\ldots$ allow one mark |  |

## Question 18: June 09 Q2

| Question Number | Scheme | Marks |
| :---: | :---: | :---: |
| Q | $\begin{aligned} & 32=2^{5} \text { or } 2048=2^{11}, \quad \sqrt{2}=2^{1 / 2} \text { or } \quad \sqrt{2048}=(2048)^{\frac{1}{2}} \\ & a=\frac{11}{2} \quad\left(\text { or } 5 \frac{1}{2} \text { or } 5.5\right) \end{aligned}$ | B1, B1 <br> B1 <br> [3] |
|  | $1^{3 t} \mathrm{~B} 1$ for $32=2^{5}$ or $2048=2^{11}$ <br> This should be explicitly seen: $32 \sqrt{2}=2^{a}$ followed by $2^{5} \sqrt{2}=2^{a}$ is OK <br> Even writing $32 \times 2=2^{5} \times 2\left(=2^{6}\right)$ is OK but simply writing $32 \times 2=2^{6}$ is NOT $2^{\text {nd }} \mathrm{B} 1$ for $2^{\frac{1}{2}}$ or $(2048)^{\frac{1}{2}}$ seen. This mark may be implied $3^{\text {rd }} \mathrm{B} 1$ for answer as written. Need $a=\ldots$ so $2^{\frac{11}{2}}$ is B0 <br> $a=\frac{11}{2}\left(\right.$ or $5 \frac{1}{2}$ or 5.5$)$ with no working scores full marks. <br> If $a=5.5$ seen then award $3 / 3$ unless it is clear that the value follows from totally incorrect work. <br> Part solutions: e.g. $2^{5} \sqrt{2}$ scores the first B1. <br> Special case: <br> If $\sqrt{2}=2^{1 / 2}$ is not explicitly seen, but the final answer includes $\frac{1}{2}$, e.g. $a=2 \frac{1}{2}, a=4 \frac{1}{2}$, the second B 1 is given by implication. |  |

Question 19: Jan 10 Q2

| Question number | Scheme | Marks |
| :---: | :---: | :---: |
|  | $\begin{align*} \text { (a) } \begin{aligned} (7+\sqrt{ } 5)(3-\sqrt{5})=21-5+ & 3 \sqrt{ } 5-7 \sqrt{ } 5 \quad \text { Expand to get } 3 \text { or } 4 \text { terms } \\ =16,-4 \sqrt{ } 5 & \left(1^{\text {th }} \mathrm{A} \text { for } 16, \quad 2^{\text {nd }} \mathrm{A} \text { for }-4 \sqrt{ } 5\right) \\ & \text { (i.s.w. if necessary, e.g. } 16-4 \sqrt{ } 5 \rightarrow 4-\sqrt{ } 5) \end{aligned} \end{align*}$ | M1 A1, A1 |
|  | (b) $\frac{7+\sqrt{5}}{3+\sqrt{5}} \times \frac{3-\sqrt{5}}{3-\sqrt{5}}$ (This is sufficient for the $M$ mark) <br> Correct denominator without surds, i.e. $9-5$ or 4 $4-\sqrt{5}$ or $4-1 \sqrt{5}$ | M1 <br> A1 <br> A1 <br> (3) <br> [6] |
|  | (a) M1: Allowed for an attempt giving 3 or 4 terms, with at least 2 correct (even if unsimplified). <br> e.g. $21-\sqrt{5^{2}}+\sqrt{15}$ scores M1. <br> Answer only: $16-4 \sqrt{ } 5$ scores full marks <br> One term correct scores the M mark by implication, <br> e.g. $26-4 \sqrt{ } 5$ scores M1 A0 A1 <br> (b) Answer only: $4-\sqrt{5}$ scores full marks <br> One term correct scores the M mark by implication, <br> e.g. $4+\sqrt{ } 5$ scores M1 A0 A0 <br> $16-\sqrt{5}$ scores M1 A0 A0 <br> Ignore subsequent working, e.g. $4-\sqrt{5}$ so $a=4, b=1$ <br> Note that, as always, A marks are dependent upon the preceding $M$ mark, so that, for example, $\frac{7+\sqrt{ } 5}{3+\sqrt{5}} \times \frac{3+\sqrt{5}}{3-\sqrt{5}}=\frac{\cdots \ldots \text {.... }}{4}$ is M0 A0. <br> Alternative <br> $(a+b \sqrt{ } 5)(3+\sqrt{ } 5)=7+\sqrt{ } 5$, then form simultaneous equations in $a$ and $b$. M1 <br> Correct equations: $\begin{array}{cccc} 3 a+5 b=7 & \text { and } & 3 b+a=1 & \text { A1 } \\ a=4 & \text { and } & b=-1 & \text { A1 } \end{array}$ |  |

Question 20: June 10 Q1


## Question 21: Jan 11 Q1

| Question Number | Scheme | Marks |
| :---: | :---: | :---: |
| (a) | $\begin{aligned} & 16^{\frac{1}{4}}=2 \text { or } \frac{1}{16^{\frac{1}{4}}} \text { or better } \\ & \qquad\left(16^{-\frac{1}{4}}=\right) \frac{1}{2} \text { or } 0.5 \end{aligned}$ | M1 <br> A1 |
| (b) | $\left(2 x^{-\frac{1}{4}}\right)^{4}=2^{4} x^{\frac{-4}{4}}$ or $\frac{2^{4}}{x^{\frac{4}{4}}}$ or equivalent $x\left(2 x^{-\frac{1}{4}}\right)^{4}=2^{4} \text { or } 16$ | M1 <br> A1 cao |
|  | Notes |  |
| (a) | M1 for a correct statement dealing with the $\frac{1}{4}$ or the - power <br> This may be awarded if 2 is seen or for reciprocal of their $16^{\frac{1}{4}}$ <br> s.c $1 / 4$ is M1 A0, also $2^{-1}$ is M1 A0 <br> $\pm \frac{1}{2}$ is not penalised so M1 A1 <br> M1 for correct use of the power 4 on both the 2 and the $x$ terms <br> A1 for cancelling the $x$ and simplifying to one of these two forms. <br> Correct answers with no working get full marks |  |

Question 22: Jan 11 Q3

\begin{tabular}{|c|c|c|}
\hline Question Number \& Scheme \& Marks <br>
\hline \& $$
\begin{aligned}
& \frac{5-2 \sqrt{3}}{\sqrt{3}-1} \times \frac{(\sqrt{3}+1)}{(\sqrt{3}+1)} \\
& =\frac{\cdots}{2} \quad \text { denominator of } 2 \\
& \text { Numerator }=5 \sqrt{3}+5-2 \sqrt{3} \sqrt{3}-2 \sqrt{3} \\
& \text { So } \frac{5-2 \sqrt{3}}{\sqrt{3}-1}=-\frac{1}{2}+\frac{3}{2} \sqrt{3}
\end{aligned}
$$ \& M1
A1

M1

A1 <br>

\hline \& | Alternative: $(p+q \sqrt{3})(\sqrt{3}-1)=5-2 \sqrt{3}$, and form simultaneous equations in $p$ and $q$ $-p+3 q=5 \text { and } p-q=-2$ |
| :--- |
| Solve simultaneous equations to give $p=-\frac{1}{2}$ and $q=\frac{3}{2}$. | \& | M1 |
| :--- |
| A1 |
| M1 A1 | <br>

\hline \& Notes \& <br>

\hline \& \multicolumn{2}{|l|}{| $1^{\text {st }} \mathrm{M} 1$ for multiplying numerator and denominator by same correct expression |
| :--- |
| $1^{\text {st }}$ A1 for a correct denominator as a single number (NB depends on M mark) |
| $2^{\text {nd }}$ M1 for an attempt to multiply the numerator by $(\sqrt{3} \pm 1)$ and get 4 terms with at least 2 correct. |
| $2^{\text {nd }} \mathrm{A} 1$ for the answer as written or $p=-\frac{1}{2}$ and $q=\frac{3}{2}$. Allow -0.5 and 1.5 . (Apply isw if correct answer seen, then slip writing $p=, q=$ ) |} <br>

\hline \& Answer only (very unlikely) is full marks if correct - no part marks \& <br>
\hline
\end{tabular}

## Question 23: June 11 Q1

| Question Number | Scheme | Marks |
| :---: | :---: | :---: |
| (a) | $5 \quad($ or $\pm 5)$ | B1 (1) |
| (b) | $25^{\frac{3}{2}}=\frac{1}{25^{\frac{3}{2}}}$ or $25^{\frac{3}{2}}=125$ or better $\frac{1}{125} \text { or } 0.008 \quad\left(\text { or } \pm \frac{1}{125}\right)$ | M1 A1 |
|  | Notes <br> (a) Give B1 for 5 or $\pm 5$ Anything else is B0 (including just -5) <br> (b) M: Requires reciprocal OR $25^{\frac{3}{2}}=125$ <br> Accept $\frac{1}{5}, \frac{1}{\sqrt{15625}}, \frac{1}{236}, \frac{1}{25 \sqrt{25}}, \frac{1}{\sqrt{33}}$ for M1 <br> Correct answer with no working (or notation errors in working) scores both marks M1A0 for $-\frac{1}{125}$ without $+\frac{1}{125}$ | i.e. M1 A1 |

Question 24: June 11 Q6

| Question <br> Number | Scheme | Marks |
| :---: | :---: | :--- |
| (a) | $p=\frac{1}{2}, q=2$ or $6 x^{\frac{1}{2}}, 3 x^{2}$ | B1, B1 |
|  | Notes |  |
|  | (a) Accept any equivalent answers, e.g. $p=0.5, q=4 / 2$ |  |

