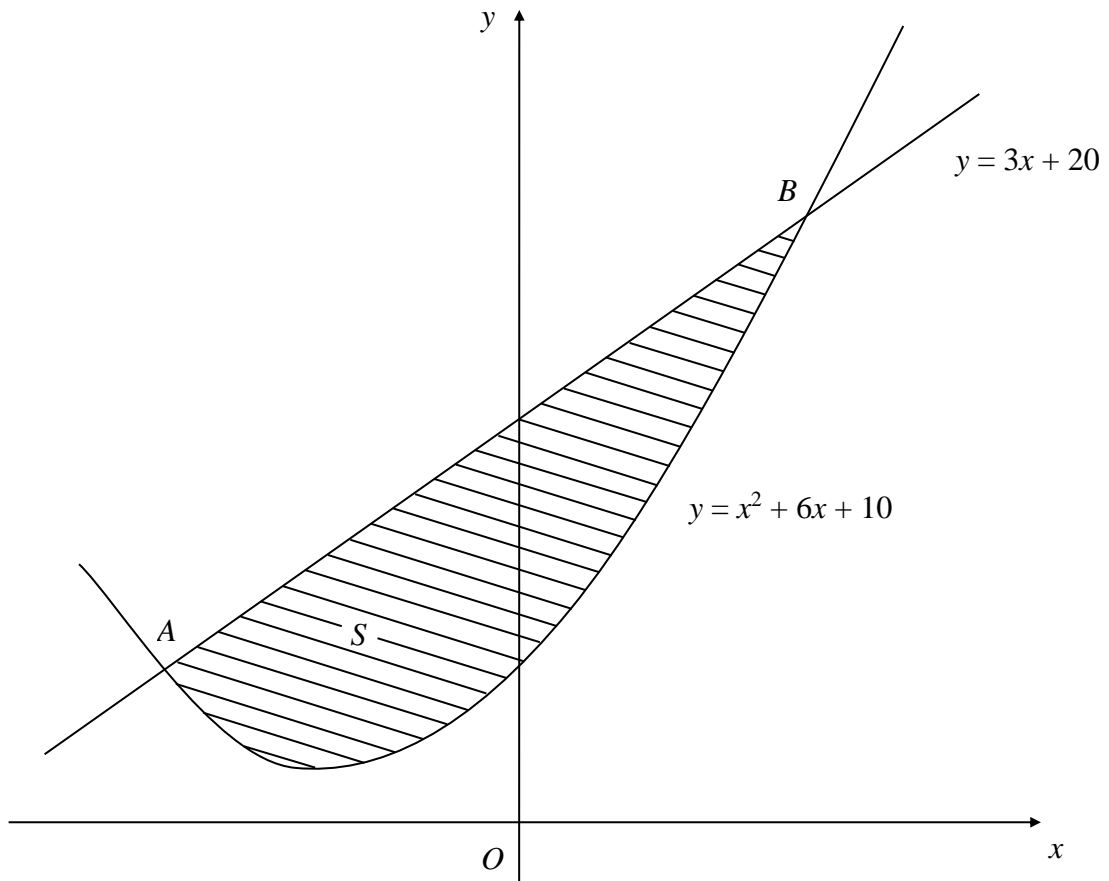


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**Integration : Area and Definite Integrals - Edexcel Past Exam Questions**

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1.



The line with equation  $y = 3x + 20$  cuts the curve with equation  $y = x^2 + 6x + 10$  at the points  $A$  and  $B$ , as shown in Figure 2.

(a) Use algebra to find the coordinates of  $A$  and the coordinates of  $B$ . (5)

The shaded region  $S$  is bounded by the line and the curve, as shown in Figure 2.

(b) Use calculus to find the exact area of  $S$ . (7)

**Jan 05 Q8**

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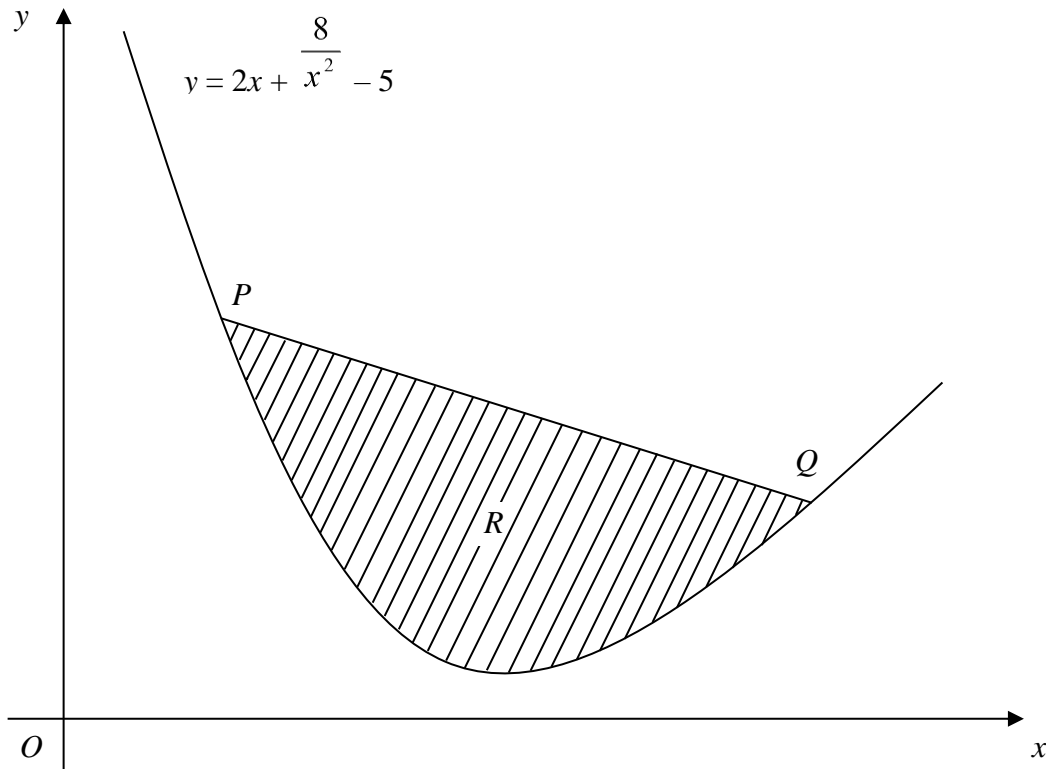
2. **Figure 1**


Figure 1 shows part of a curve  $C$  with equation  $y = 2x + \frac{8}{x^2} - 5$ ,  $x > 0$ .

The points  $P$  and  $Q$  lie on  $C$  and have  $x$ -coordinates 1 and 4 respectively. The region  $R$ , shaded in Figure 1, is bounded by  $C$  and the straight line joining  $P$  and  $Q$ .

(a) Find the exact area of  $R$ . (8)

(b) Use calculus to show that  $y$  is increasing for  $x > 2$ . (4)

**June 05 Q10**

3.

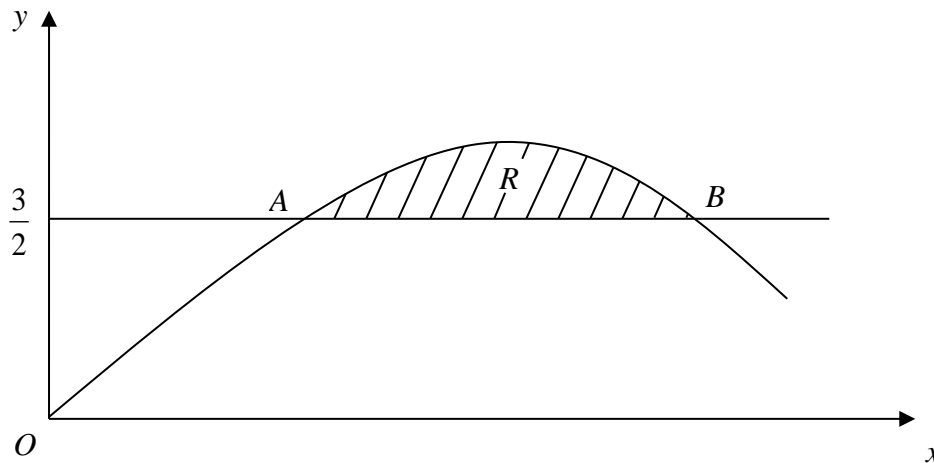


Figure 3

Figure 3 shows the shaded region  $R$  which is bounded by the curve  $y = -2x^2 + 4x$  and the line  $y = \frac{3}{2}$ . The points  $A$  and  $B$  are the points of intersection of the line and the curve.

Find

(a) the  $x$ -coordinates of the points  $A$  and  $B$ , (4)

(b) the exact area of  $R$ . (6)

**Jan 06 Q9**

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4. Use calculus to find the exact value of  $\int_1^2 \left( 3x^2 + 5 + \frac{4}{x^2} \right) dx$ . (5)

**June 06 Q2**

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5.  $f(x) = x^3 + 3x^2 + 5$ .

Find

(a)  $f''(x)$ , (3)

(b)  $\int_1^2 f(x) dx$  (4)

**Jan 07 Q1**

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6.

Figure 3

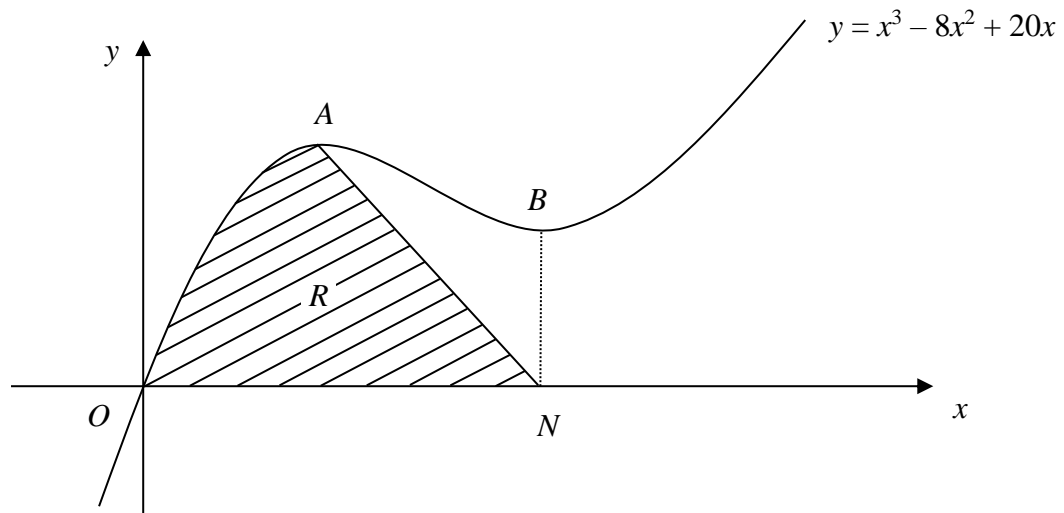


Figure 3 shows a sketch of part of the curve with equation  $y = x^3 - 8x^2 + 20x$ . The curve has stationary points A and B.

(a) Use calculus to find the  $x$ -coordinates of A and B. (4)

(b) Find the value of  $\frac{d^2y}{dx^2}$  at A, and hence verify that A is a maximum. (2)

The line through B parallel to the  $y$ -axis meets the  $x$ -axis at the point N. The region R, shown shaded in Figure 3, is bounded by the curve, the  $x$ -axis and the line from A to N.

(c) Find  $\int (x^3 - 8x^2 + 20x) dx$ . (3)

(d) Hence calculate the exact area of R. (5)

June 06 Q10

7.

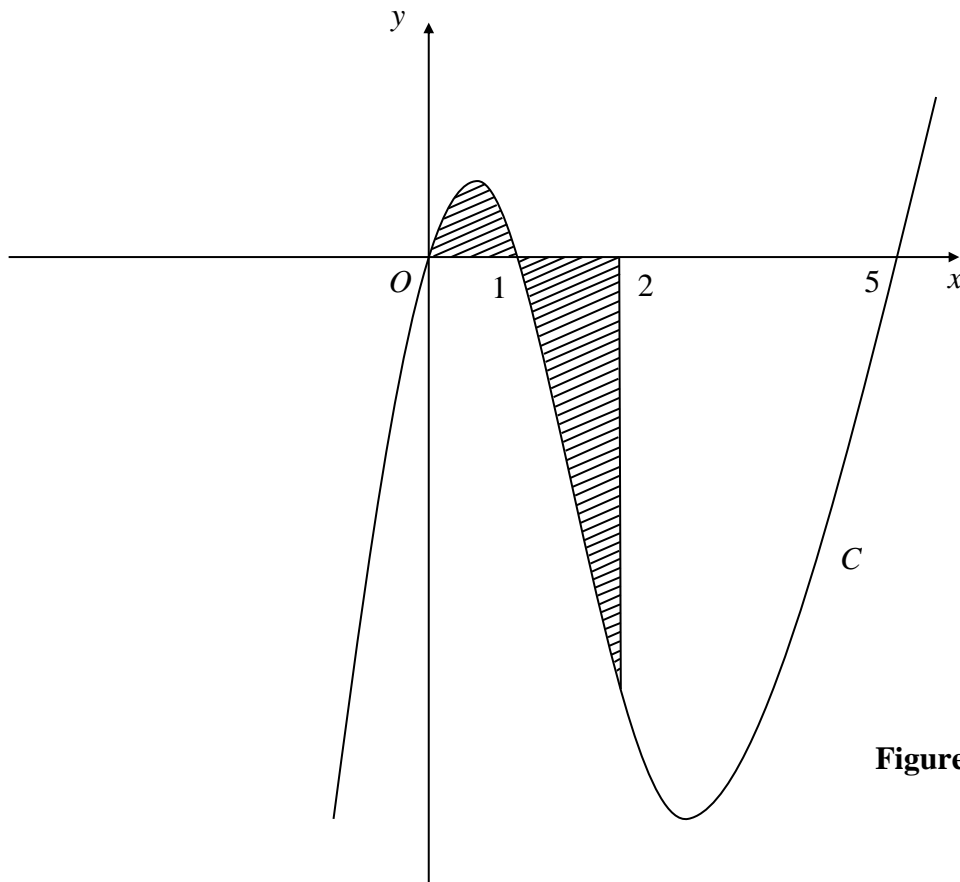


Figure 1

Figure 1 shows a sketch of part of the curve  $C$  with equation

$$y = x(x - 1)(x - 5).$$

Use calculus to find the total area of the finite region, shown shaded in Figure 1, that is between  $x = 0$  and  $x = 2$  and is bounded by  $C$ , the  $x$ -axis and the line  $x = 2$ .

(9)

Jan 07 Q7

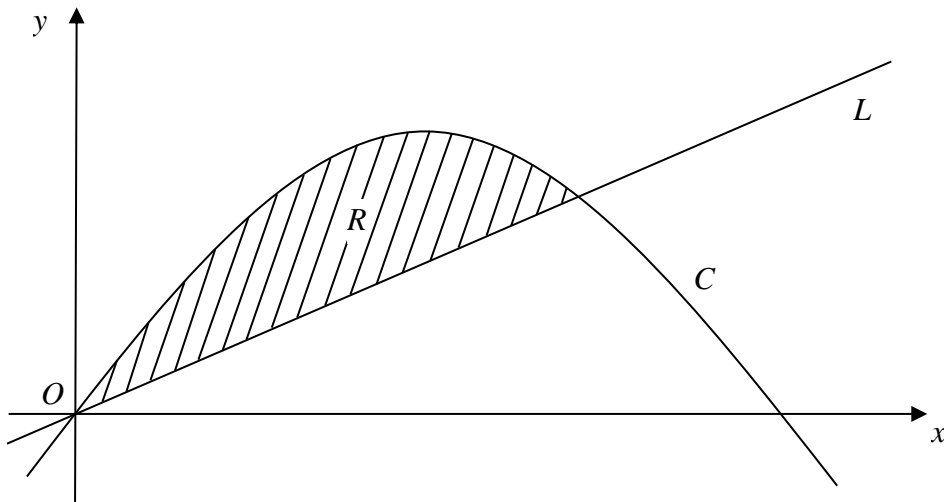
8. Evaluate  $\int_1^8 \frac{1}{\sqrt{x}} dx$ , giving your answer in the form  $a + b\sqrt{2}$ , where  $a$  and  $b$  are integers.

(4)

June 07 Q1

9.

Figure 2



In Figure 2 the curve  $C$  has equation  $y = 6x - x^2$  and the line  $L$  has equation  $y = 2x$ .

(a) Show that the curve  $C$  intersects with the  $x$ -axis at  $x = 0$  and  $x = 6$ . (1)

(b) Show that the line  $L$  intersects the curve  $C$  at the points  $(0, 0)$  and  $(4, 8)$ . (3)

The region  $R$ , bounded by the curve  $C$  and the line  $L$ , is shown shaded in Figure 2.

(c) Use calculus to find the area of  $R$ . (6)

**Jan 08 Q7**

10.

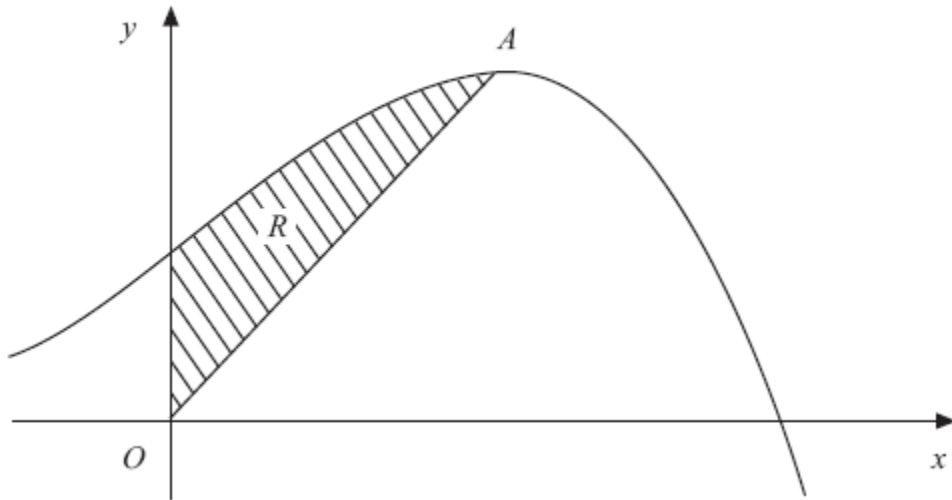
**Figure 2**

Figure 2 shows a sketch of part of the curve with equation  $y = 10 + 8x + x^2 - x^3$ .

The curve has a maximum turning point  $A$ .

(a) Using calculus, show that the  $x$ -coordinate of  $A$  is 2. (3)

The region  $R$ , shown shaded in Figure 2, is bounded by the curve, the  $y$ -axis and the line from  $O$  to  $A$ , where  $O$  is the origin.

(b) Using calculus, find the exact area of  $R$ . (8)

**June 08 Q8**

11.

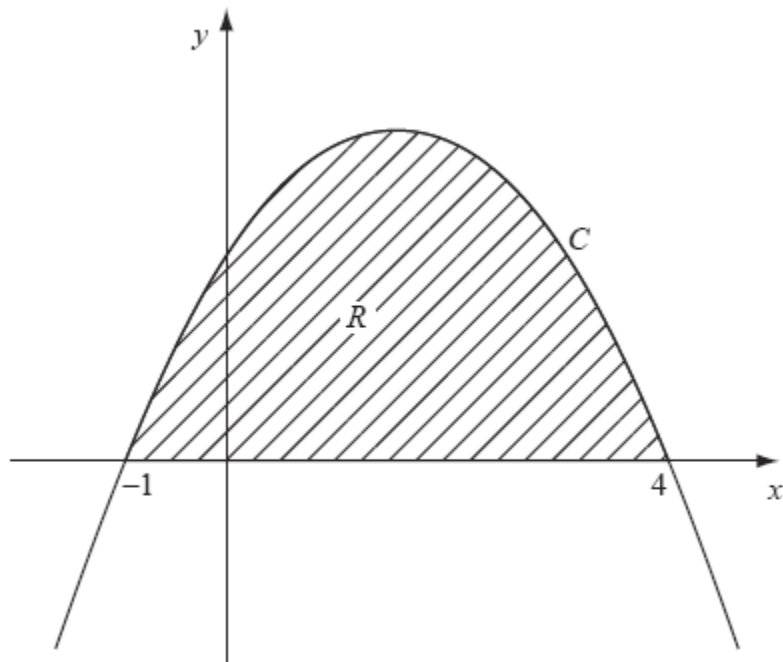
**Figure 1**

Figure 1 shows part of the curve  $C$  with equation  $y = (1 + x)(4 - x)$ .

The curve intersects the  $x$ -axis at  $x = -1$  and  $x = 4$ . The region  $R$ , shown shaded in Figure 1, is bounded by  $C$  and the  $x$ -axis.

Use calculus to find the exact area of  $R$ .

(5)

**Jan 09 Q2**

12. Use calculus to find the value of

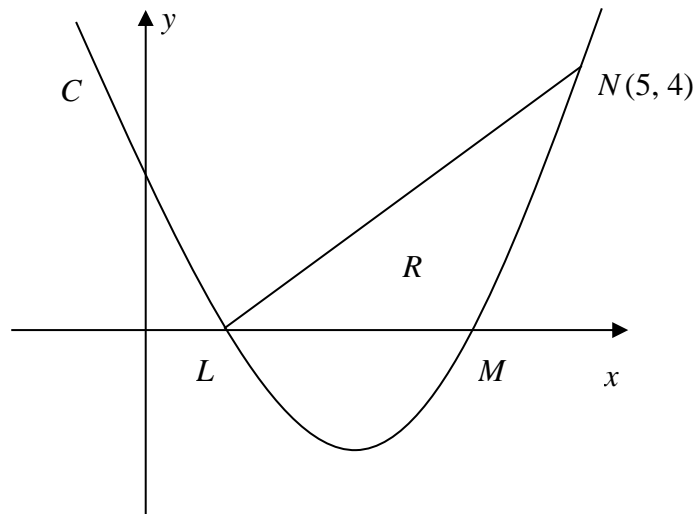
$$\int_1^4 (2x + 3\sqrt{x}) \, dx.$$

(5)

**June 09 Q1**



13.

**Figure 2**

The curve  $C$  has equation  $y = x^2 - 5x + 4$ . It cuts the  $x$ -axis at the points  $L$  and  $M$  as shown in Figure 2.

(a) Find the coordinates of the point  $L$  and the point  $M$ . (2)

(b) Show that the point  $N(5, 4)$  lies on  $C$ . (1)

(c) Find  $\int (x^2 - 5x + 4) \, dx$ . (2)

The finite region  $R$  is bounded by  $LN$ ,  $LM$  and the curve  $C$  as shown in Figure 2.

(d) Use your answer to part (c) to find the exact value of the area of  $R$ . (5)

**Jan 10 Q7**

14.

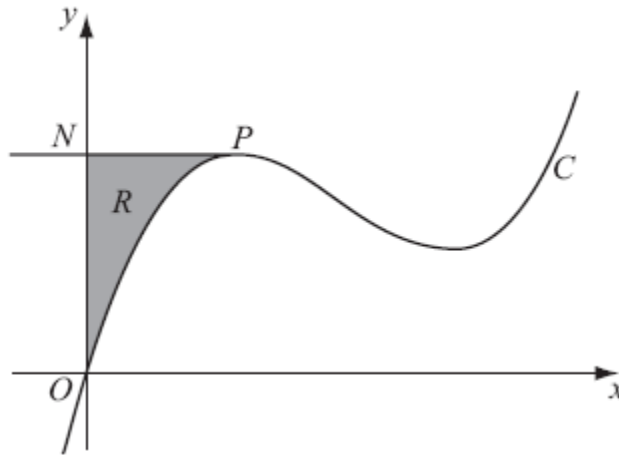

**Figure 2**

Figure 2 shows a sketch of part of the curve  $C$  with equation

$$y = x^3 - 10x^2 + kx,$$

where  $k$  is a constant.

The point  $P$  on  $C$  is the maximum turning point.

Given that the  $x$ -coordinate of  $P$  is 2,

(a) show that  $k = 28$ . (3)

The line through  $P$  parallel to the  $x$ -axis cuts the  $y$ -axis at the point  $N$ .  
The region  $R$  is bounded by  $C$ , the  $y$ -axis and  $PN$ , as shown shaded in Figure 2.

(b) Use calculus to find the exact area of  $R$ . (6)

**June 10 Q8**

15.

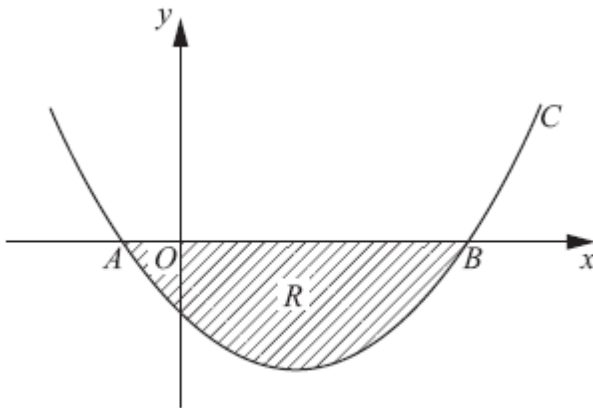


Figure 1

Figure 1 shows a sketch of part of the curve  $C$  with equation

$$y = (x + 1)(x - 5).$$

The curve crosses the  $x$ -axis at the points  $A$  and  $B$ .

(a) Write down the  $x$ -coordinates of  $A$  and  $B$ . (1)

The finite region  $R$ , shown shaded in Figure 1, is bounded by  $C$  and the  $x$ -axis.

(b) Use integration to find the area of  $R$ . (6)

**Jan 11 Q4**

16.

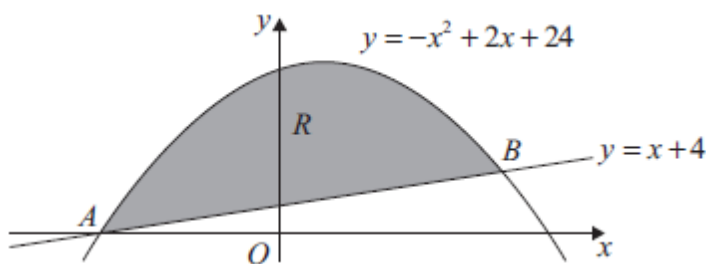


Figure 3

The straight line with equation  $y = x + 4$  cuts the curve with equation  $y = -x^2 + 2x + 24$  at the points  $A$  and  $B$ , as shown in Figure 3.

(a) Use algebra to find the coordinates of the points  $A$  and  $B$ . (4)

The finite region  $R$  is bounded by the straight line and the curve and is shown shaded in Figure 3.

(b) Use calculus to find the exact area of  $R$ . (7)

**June 11 Q9**