Solving Equations using Logarithms - Edexcel Past Exam Questions ${\it MARK}$ SCHEME

Question 1: Jan 05 Q3

| Question Number | Scheme | Marks |
|--------------------|--|------------|
| -, | $(a)\log 3^x = \log 5$ | M1 |
| | $x = \frac{\log 5}{\log 3}$ | A1 |
| | <u>= 1.46</u> | A1 cao (3) |
| | (b) $\log_2(\frac{2x+1}{x}) = 2$ $\frac{2x+1}{x} = 2^2 \text{ or } 4$ | M1 |
| | $\frac{2x+1}{x} = 2^2 \text{ or } 4$ | M1 |
| | 2x + 1 = 4x | M1 |
| | $x = \frac{1}{2}$ or 0.5 | A1 (4) |
| | | (7) |
| | (a) M1 a correct attempt to take logs | |
| | Al an exact expression for x that can be evaluated on a calculator | |
| | e.g. $x = \log_3 5$ scores M1 A0 | |
| | (b) 1^{st} M1 for use of $\log a(\pm) \log b$ rule | |
| | 2 nd M1 for getting out of logs | |
| | $3^{\rm rd}$ M1 forming and solving a linear equation $\rightarrow x = \alpha$ | |
| | A1 $\alpha = \frac{1}{2}$ or 0.5 | |
| | 2 | |



Question 2 : June 05 Q2

| Question number | Scheme | Marks |
|--------------------|--|----------------|
| 2. | (a) $x \log 5 = \log 8$, $x = \frac{\log 8}{\log 5}$, $= 1.29$ | M1, A1, A1 (3) |
| | (b) $\log_2 \frac{x+1}{x}$ (or $\log_2 7x$) | B1 |
| | $\frac{x+1}{x} = 7 \qquad x = \dots, \qquad \frac{1}{6} \qquad \text{(Allow 0.167 or better)}$ | M1, A1 (3) |
| | | 6 |
| | (a) Answer only 1.29: Full marks. | |
| | Answer only, which rounds to 1.29 (e.g. 1.292): M1 A1 A0 | |
| | Answer only, which rounds to 1.3: M1 A0 A0 | |
| | Trial and improvement: Award marks as for "answer only". | |
| | (b) M1: Form (by legitimate log work) and solve an equation in x . | |
| | Answer only: No marks unless verified (then full marks are available). | |

Question 3: June 06 Q3

| Question number | Scheme | Marks | |
|--------------------|--|--------|-----|
| 3. | (i) 2 | B1 | (1) |
| | (ii) $2\log 3 = \log 3^2$ (or $2\log p = \log p^2$) | B1 | |
| | $\log_a p + \log_a 11 = \log_a 11p$, $= \log_a 99$ (Allow e.g. $\log_a (3^2 \times 11)$) | M1, A1 | (3) |
| | | | 4 |
| | (ii) Ignore 'missing base' or wrong base. | | |
| | The correct answer with no working scores full marks. | | |
| | $\log_a 9 \times \log_a 11 = \log_a 99$, or similar mistakes, score M0 A0. | | |



Question 4: Jan 07 Q4

| Question Number | Scheme | Marks |
|--------------------|---|--------|
| 4. | $x\log 5 = \log 17 \qquad \qquad \text{or} \qquad \qquad x = \log_5 17$ | M1 |
| | $x = \frac{\log 17}{\log 5}$ | A1 |
| | = 1.76 | A1 (3) |

 $\underline{\text{Notes}}$ N.B. It is never possible to award an A mark after giving M0. If M0 is given then the marks will be M0 A0 A0.

| 4 | |
|--|--------|
| Acceptable alternatives include | 1st M1 |
| $x \log 5 = \log 17$; $x \log_{10} 5 = \log_{10} 17$; $x \log_{e} 5 = \log_{e} 17$; $x \ln 5 = \ln 17$; $x = \log_{5} 17$ | |
| Can be implied by a correct exact expression as shown on the first A1 mark | |
| An exact expression for x that can be evaluated on a calculator. Acceptable alternatives include | 1st A1 |
| $x = \frac{\log 17}{\log 5}$; $x = \frac{\log_{10} 17}{\log_{10} 5}$; $x = \frac{\log_e 17}{\log_e 5}$; $x = \frac{\ln 17}{\ln 5}$; $x = \frac{\log_q 17}{\log_q 5}$ where q is a number | |
| This may not be seen (as, for example, $\log_5 17$ can be worked out directly on many calculators) so this A mark can be implied by the correct final answer or the right answer corrected to or truncated to a greater accuracy than 3 significant figures or 1.8 | |
| Alternative: $x = \frac{\text{a number}}{\text{a number}}$ where this fraction, when worked out as a decimal rounds to 1.76. | |
| (N.B. remember that this A mark cannot be awarded without the M mark). | |
| If the line for the M mark is missing but this line is seen (with or without the $x = $) and is <u>correct</u> | |
| the method can be assumed and M1 1st A1 given. | |
| 1.76 cao | 2nd A1 |
| N.B. $\sqrt[5]{17} = 1.76$ and $x^5 = 17$, $\therefore x = 1.76$ are both M0 A0 A0 | |
| Answer only 1.76: full marks (M1 A1 A1) | |
| Answer only to a greater accuracy but which rounds to 1.76: M1 A1 A0 | |
| (e.g. 1.760, 1.7603, 1.7604, 1.76037 etc) | |
| Answer only 1.8: M1 A1 A0 | |
| Trial and improvement: award marks as for "answer only". | |



Question 5 : June 07 Q6

| Question number | Scheme | | Marks | s |
|--------------------|---|----------------------|--------|----------|
| | (a) $x = \frac{\log 0.8}{\log 8}$ or $\log_8 0.8$, $= -0.107$ Allow | awrt | M1, A1 | (2) |
| | (b) $2\log x = \log x^2$ | | B1 | |
| | $\log x^2 - \log 7x = \log \frac{x^2}{7x}$ | | M1 | |
| | "Remove logs" to form equation in x , using the base correctly: | $\frac{x^2}{7x} = 3$ | M1 | |
| | x = 21 (Ignore $x = 0$) | , if seen) | A1cso | (4) 6 |
| | (a) Allow also the 'implicit' answer $8^{-0.107}$ (M1 A1). | | | |
| | Answer only: -0.107 or awrt: Full marks. | | | |
| | Answer only: -0.11 or awrt (insufficient accuracy): M1 A0 | | | |
| | Trial and improvement: Award marks as for "answer only". | | | |
| | (b) Alternative: | | | |
| | $2\log x = \log x^2$ | B1 | | |
| | $\log 7x + 1 = \log 7x + \log 3 = \log 21x$ | M1 | | |
| | "Remove logs" to form equation in x: $x^2 = 21x$ x = 21 (Ignore $x = 0$) | M1 | | |
| | Alternative: | , it seen). At | | |
| | $\log 7x = \log 7 + \log x$ | B1 | | |
| | $2\log x - (\log 7 + \log x) = 1$ | M | | |
| | $\log_3 x = 1 + \log_3 7$ | M1 | | |
| | $x = 3^{(1+\log_3 7)}$ (= $3^{2.771}$) or $\log_3 x = \log_3 3 + \log_3 7$ x = 21 | M1 A1 | | |
| | Attempts using change of base will usually require the same st main scheme or alternatives, so can be marked equivalently. | | | |
| | A common mistake: | | | |
| | $\log x^{2} - \log 7x = \frac{\log x^{2}}{\log 7x}$ B1 M0 $\frac{x^{2}}{7x} = 3$ $x = 21$ M1('Recovery'), but | | | |
| | $\frac{x^2}{7x} = 3 	 x = 21 	 M1('Recovery'), but$ | A0 | | |
| | | | | |



Question 6: Jan 08 Q5

| Question Number | Scheme | | Marks |
|--------------------|---|---|----------|
| Number | Method 1 (Substituting a = 3b into second equation | at some stage) | |
| | Using a law of logs correctly (anywhere) | e.g. $\log_3 ab = 2$ | М1 |
| | Substitution of 3b for a (or a/3 for b) | e.g. $\log_3 3b^2 = 2$ | М1 |
| | Using base correctly on correctly derived log ₃ p= q | e.g. $3b^2 = 3^2$ | M1 |
| | First correct value | $b = \sqrt{3} \text{ (allow 3}^{\frac{1}{2}})$ | A1 |
| | Correct method to find other value (dep. on at least | first M mark) | М1 |
| | Second answer | $a = 3b = 3 \sqrt{3} \text{ or } \sqrt{27}$ | A1 |
| | Method 2_(Working with two equations in log₃a_and | log₃b) | |
| | " Taking logs" of first equation and " separating" | $\log_3 a = \log_3 3 + \log_3 b$ $(= 1 + \log_3 b)$ | М1 |
| | Solving simultaneous equations to find $\log_3 a$ or $\log_3 a = 1\frac{1}{2}$, $\log_3 b = \frac{1}{2}$ | ₃ b | M1 |
| | Using base correctly to find a or b | | M1 |
| | Correct value for a or b $a = a$ | $3\sqrt{3}$ or $b=\sqrt{3}$ | A1 |
| | Correct method for second answer, dep. on first M; of [Ignore negative values] | correct second answer | M1;A1[6] |



| Notes: | Answers must be exact; decimal answers lose both A marks |
|--------|---|
| | There are several variations on Method 1, depending on the stage at which |
| | a = 3b is used, but they should all mark as in scheme. |
| | In this method, the first three method marks on Epen are for |
| | (i) First M1: correct use of log law, |
| | (ii) Second M1: substitution of a = 3b, |
| | (iii) Third M1: requires using base correctly on correctly derived log₃ p= q |
| | Three examples of applying first 4 marks in Method 1: (i) $\log_3 3b + \log_3 b = 2$ gains second M1 $\log_3 3 + \log_3 b + \log_3 b = 2$ gains first M1 $(2\log_3 b = 1, \log_3 b = \frac{1}{2})$ no mark yet |
| | $b = 3^{\frac{1}{2}}$ gains third M1, and if correct A1 |
| | (ii) $log_3(ab) = 2$ gains first M1 |
| | $ab = 3^2$ gains third M1 |
| | $3b^2 = 3^2$ gains second M1 |
| | (iii) $\log_3 3b^2 = 2$ has gained first 2 M marks |
| | $\Rightarrow 2\log_3 3b = 2$ or similar type of error |
| | $\Rightarrow \log_3 3b = 1 \Rightarrow 3b = 3$ does not gain third M1, as $\log_3 3b = 1$ |
| | not derived correctly |
| | |

Question 7: June 08 Q4

| Question Number | Scheme | Marks |
|--------------------|--|-----------|
| (a) | $x = \frac{\log 7}{\log 5} \text{or} x = \log_5 7$ | M1 |
| | 1.21 | A1 (2) |
| (b) | $(5^x - 7)(5^x - 5)$ $(5^x = 7 \text{ or } 5^x = 5)$ $x = 1.2 \text{ (awrt)}$ | M1 A1 |
| | $(5^x = 7 \text{ or } 5^x = 5)$ $x = 1.2 \text{ (awrt)}$ | A1 ft |
| | x = 1 | B1 (4) |
| | | (6 marks) |



Question 8: Jan 09 Q4

| Question Number | Scheme | Marks |
|--------------------|---|-----------------|
| | $2\log_5 x = \log_5(x^2), \qquad \log_5(4-x) - \log_5(x^2) = \log_5 \frac{4-x}{x^2}$ $\log\left(\frac{4-x}{x^2}\right) = \log 5 \qquad 5x^2 + x - 4 = 0 \text{ or } 5x^2 + x = 4 \text{ o.e.}$ | B1, M1 |
| | $\log\left(\frac{4-x}{x^2}\right) = \log 5$ $5x^2 + x - 4 = 0$ or $5x^2 + x = 4$ o.e. | M1 A1 |
| | $(5x-4)(x+1) = 0$ $x = \frac{4}{5}$ $(x = -1)$ | dM1 A1 (6) |
| Notes | B1 is awarded for $2 \log x = \log x^2$ anywhere. M1 for correct use of $\log A - \log B = \log \frac{A}{B}$ M1 for replacing 1 by $\log_k k$. A1 for correct quadratic | |
| | $(\log(4-x) - \log x^2 = \log 5 \Rightarrow 4-x-x^2 = 5 \text{ is B1M0M1A0 M0A0})$ | |
| | dM1 for attempt to solve quadratic with usual conventions. (Only award M marks have been awarded) Al for 4/5 or 0.8 or equivalent (Ignore extra answer). | if previous two |
| Alternative | $\log_5(4-x)-1=2\log_5 x$ so $\log_5(4-x)-\log_5 5=2\log_5 x$ | M1 |
| 1 | $\log_5 \frac{4-x}{5} = 2\log_5 x$ | M1 |
| | then could complete solution with $2\log_5 x = \log_5(x^2)$ | B1 |
| | $\left(\frac{4-x}{5}\right) = x^2 \qquad 5x^2 + x - 4 = 0$ | A1 |
| | Then as in first method $(5x-4)(x+1) = 0$ $x = \frac{4}{5}$ $(x = -1)$ | dM1 A1 (6) |
| Special cases | Complete trial and error yielding 0.8 is M3 and B1 for 0.8 A1, A1 awarded for each of two tries evaluated. i.e. 6/6 Incomplete trial and error with wrong or no solution is 0/6 Just answer 0.8 with no working is B1 If log base 10 or base e used throughout - can score B1M1M1A0M1A0 | |

Question 9: June 09 Q8

| Question Number | Scheme | Mar | rks |
|--------------------|--|--------------|----------|
| Q (a) | $\log_2 y = -3 \Rightarrow y = 2^{-3}$ | M1 | |
| | $y = \frac{1}{9} \text{or} 0.125$ | A1 | (2 |
| (b) | $32 = 2^5$ or $16 = 2^4$ or $512 = 2^9$ | M1 | |
| | [or $\log_2 32 = 5\log_2 2$ or $\log_2 16 = 4\log_2 2$ or $\log_2 512 = 9\log_2 2$] | | |
| | [or $\log_2 32 = \frac{\log_{10} 32}{\log_{10} 2}$ or $\log_2 16 = \frac{\log_{10} 16}{\log_{10} 2}$ or $\log_2 512 = \frac{\log_{10} 512}{\log_{10} 2}$] | | |
| | $\log_2 32 + \log_2 16 = 9$ | A1 | |
| | $(\log x)^2 = \dots$ or $(\log x)(\log x) = \dots$ (May not be seen explicitly, so M1 may be implied by later work, and the base may be 10 rather than 2) | M1 | |
| | $\log_2 x = 3 \Rightarrow x = 2^3 = 8$ | A1 | |
| | $\log_2 x = -3 \Rightarrow x = 2^{-3} = \frac{1}{8}$ | A1ft | (5 [7 |
| (b) | scores M1. A1 for the exact answer, e.g. $\log_{10} y = -0.903 \Rightarrow y = 0.12502$ scores M1 (implied Correct answer with no working scores both marks. Allow both marks for implicit statements such as $\log_2 0.125 = -3$. 1st M1 for expressing 32 or 16 or 512 as a power of 2, or for a change of base enabling evaluation of $\log_2 32$, $\log_2 16$ or $\log_2 512$ by calculator. (Can be implied by 5, 4 or 9 respectively). 1st A1 for 9 (exact). 2nd M1 for getting $(\log_2 x)^2 = \text{constant}$. The constant can be a log or a sum of logs. If written as $\log_2 x^2$ instead of $(\log_2 x)^2$, allow the M mark only if subsequent work implies correct interpretation. 2nd A1 for 8 (exact). Change of base methods leading to a non-exact answer score A0 3^{rd} A1ft for an answer of $\frac{1}{\text{their } 8}$. An ft answer may be non-exact. Possible mistakes: $\log_2(2^9) = \log_2(x^2) \Rightarrow x^2 = 2^9 \Rightarrow x =$ scores M1A1(implied by 9)M0A0A0 $\log_2 512 = \log_2 x \times \log_2 x \Rightarrow x^2 = 512 \Rightarrow x =$ scores M0A0(9 never seen)M1A0A1 $\log_2 48 = (\log_2 x)^2 \Rightarrow (\log_2 x)^2 = 5.585 \Rightarrow x = 5.145, x = 0.194$ scores M0A0M1A | ng t t | |

Question 10: Jan 10 Q5

| Question Number | Scheme | Mar | ks |
|--------------------|--|-----|-----|
| (a) | $\log_x 64 = 2 \implies 64 = x^2$ | M1 | |
| | So $x = 8$ | A1 | (2) |
| (b) | $\log_2(11-6x) = \log_2(x-1)^2 + 3$ | M1 | |
| | $\log_2\left[\frac{11-6x}{\left(x-1\right)^2}\right] = 3$ | M1 | |
| | $\frac{11-6x}{(x-1)^2} = 2^3$ | M1 | |
| | $\{11-6x=8(x^2-2x+1)\}$ and so $0=8x^2-10x-3$ | A1 | |
| | $0 = (4x+1)(2x-3) \implies x = \dots$ | dM1 | |
| | $x = \frac{3}{2}, \left[-\frac{1}{4} \right]$ | A1 | (6) |
| | 2 4 | | [8] |
| (a) | M1 for getting out of logs A1 Do not need to see $x = -8$ appear and get rejected. Ignore $x = -8$ as extra solution. $x = 8$ with no working is M1 A1 | | |
| (b) | 1 st M1 for using the $n\log x$ rule 2 nd M1 for using the $\log x$ - $\log y$ rule or the $\log x$ + $\log y$ rule as appropriate 3 rd M1 for using 2 to the power- need to see 2 ³ or 8 (May see 3 = $\log_2 8$ used) If all three M marks have been earned and $\log x$ are still present in equation do not give final M1. So solution stopping at $\log_2 \left[\frac{11-6x}{(x-1)^2} \right] = \log_2 8$ would earn | | |
| | M1M1M0 1 st A1 for a correct 3TQ 4 th dependent M1 for attempt to solve or factorize their 3TQ to obtain $x =$ (mark depends on three previous M marks) 2 nd A1 for 1.5 (ignore -0.25) s.c 1.5 only – no working – is 0 marks | | |
| (a) | Change base: (i) $\frac{\log_2 64}{\log_2 x} = 2$, so $\log_2 x = 3$ and $x = 2^3$, is M1 or | | |
| | (ii) $\frac{\log_{10} 64}{\log_{10} x} = 2$, $\log x = \frac{1}{2} \log 64$ so $x = 64^{\frac{1}{2}}$ is M1 then $x = 8$ is A1 BUT $\log x = 0.903$ so $x = 8$ is M1A0 (loses accuracy mark) | | |
| | (iii) $\log_{64} x = \frac{1}{2}$ so $x = 64^{\frac{1}{2}}$ is M1 then $x = 8$ is A1 | | |

Question 11: June 10 Q7

| Question Number | Scheme | Marks |
|--------------------|---|-----------|
| | (a) $2\log_3(x-5) = \log_3(x-5)^2$ | B1 |
| | $\log_3(x-5)^2 - \log_3(2x-13) = \log_3\frac{(x-5)^2}{2x-13}$ | M1 |
| | $\log_3 3 = 1$ seen or used correctly | B1 |
| | $\log_3\left(\frac{P}{Q}\right) = 1 \implies P = 3Q \left\{\frac{(x-5)^2}{2x-13} = 3 \implies (x-5)^2 = 3(2x-13)\right\}$ | M1 |
| | $x^2 - 16x + 64 = 0 		(*)$ | A1 cso (5 |
| | (b) $(x-8)(x-8) = 0 \implies x = 8$ Must be seen in part (b). | M1 A1 |
| | Or: Substitute $x = 8$ into original equation and verify. Having additional solution(s) such as $x = -8$ loses the A mark. | (2 |
| | x = 8 with no working scores both marks. | 1 |

(a) Marks may be awarded if equivalent work is seen in part (b).

1st M:
$$\log_3(x-5)^2 - \log_3(2x-13) = \frac{\log_3(x-5)^2}{\log_3(2x-13)}$$
 is M0

$$2\log_3(x-5) - \log_3(2x-13) = 2\log\frac{x-5}{2x-13}$$
 is M0

 2^{nd} M: After the first mistake above, this mark is available only if there is 'recovery' to the required $\log_3\left(\frac{P}{Q}\right) = 1 \implies P = 3Q$. Even then the final mark (cso) is lost.

'Cancelling logs', e.g.
$$\frac{\log_3(x-5)^2}{\log_3(2x-13)} = \frac{(x-5)^2}{2x-13}$$
 will also lose the 2nd M.

A typical wrong solution:

$$\log_3 \frac{(x-5)^2}{2x-13} = 1 \quad \Rightarrow \quad \log_3 \frac{(x-5)^2}{2x-13} = 3 \quad \Rightarrow \frac{(x-5)^2}{2x-13} = 3 \quad \Rightarrow \quad (x-5)^2 = 3(2x-13)$$

1

(Wrong sten here)

This, with no evidence elsewhere of log₃ 3 = 1, scores B1 M1 B0 M0 A0

However, $\log_3 \frac{(x-5)^2}{2x-13} = 1 \implies \frac{(x-5)^2}{2x-13} = 3$ is correct and could lead to full marks.

(Here $log_3 3 = 1$ is implied).

No log methods shown:

It is <u>not</u> acceptable to jump immediately to $\frac{(x-5)^2}{2x-13} = 3$. The only mark this scores is the 1st B1 (by generous implication).

(b) M1: Attempt to solve the <u>given</u> quadratic equation (usual rules), so the factors (x − 8)(x − 8) with no solution is M0.



Question 12: Jan 11 Q8

| Question Number | Scheme | Ma | rks |
|--------------------|--|-----------------------|------------|
| (a) | Graph of $y = 7^x$, $x \in \mathbb{R}$ and solving $7^{2x} - 4(7^x) + 3 = 0$ At least two of the three criteria correct. (See notes below.) All three criteria correct. (See notes below.) | B1 | (2) |
| (b) | Forming a quadratic {using $y^2 - 4y + 3 = 0$ } $y'' = 7^x$ }. $y'' = 7^x$ }. $y^2 - 4y + 3 = 0$ } { $(y-3)(y-1) = 0$ or $(7^x - 3)(7^x - 1) = 0$ } | | (=) |
| | $y=3$, $y=1$ or $7^x=3$, $7^x=1$ Both $y=3$ and $y=1$. $\{7^x=3\Rightarrow\}$ $x\log 7 = \log 3$ A valid method for solving $7^x=k$ where $k>0$, $k\neq 1$ $x=0.5645$ $x=0$ | A1 dM1 A1 B1 | (6) [8] |
| | <u>Notes</u> | | |
| (a) | B1B0: Any two of the following three criteria below correct. B1B1: All three criteria correct. Criteria number 1: Correct shape of curve for x ≥ 0. Criteria number 2: Correct shape of curve for x < 0. Criteria number 3: (0, 1) stated or 1 marked on the y-axis. Allow (1, 0) rather than (0, marked in the "correct" place on the y-axis. | 1) if | |

| Question Number | Scheme | Marks |
|--------------------|---|-----------|
| (b) | 1 st M1 is an attempt to form a quadratic equation {using " y " = 7^x .} | |
| | 1 st A1 mark is for the correct quadratic equation of $y^2 - 4y + 3 = 0$. | |
| | Can use any variable here, eg: y, x or 7^x . Allow M1A1 for $x^2 - 4x + 3 = 0$. | |
| | Writing $(7^x)^2 - 4(7^x) + 3 = 0$ is also sufficient for M1A1. | |
| | Award M0A0 for seeing $7^{x^2} - 4(7^x) + 3 = 0$ by itself without seeing $y^2 - 4y + 3 = 0$ | or |
| | $(7^x)^2 - 4(7^x) + 3 = 0.$ | |
| | 1 st A1 mark for both $y = 3$ and $y = 1$ or both $7^x = 3$ and $7^x = 1$. Do not give this according | ıracy |
| | mark for both $x = 3$ and $x = 1$, unless these are recovered in later working by candidate | |
| | applying logarithms on these. | |
| | Award M1A1A1 for $7^x = 3$ and $7^x = 1$ written down with no earlier working. | |
| | 3^{rd} dM1 for solving $7^x = k$, $k > 0$, $k \ne 1$ to give either $x \ln 7 = \ln k$ or $x = \frac{\ln k}{\ln 7}$ or $x = \log k$ | $_{7}k$. |
| | dM1 is dependent upon the award of M1. | |
| | 2^{nd} A1 for 0.565 or awrt 0.56. B1 is for the solution of $x = 0$, from any working. | |



Question 13: June 11 Q3

| Question Number | Scheme | Marks | |
|--------------------|---|----------|--|
| | (a) $5^x = 10$ and (b) $\log_3(x-2) = -1$ | | |
| (a) | $x = \frac{\log 10}{\log 5} \text{or} x = \log_5 10$ | M1 | |
| | x = 1.430676558 = 1.43 (3 sf) | A1 cao | |
| (b) | $(x-2)=3^{-1}$ $(x-2)=3^{-1}$ or $\frac{1}{3}$ | M1 oe | |
| | $x\left\{=\frac{1}{3}+2\right\}=2\frac{1}{3}$ $2\frac{1}{3}$ or $\frac{7}{3}$ or 2.3 or awrt 2.33 | A1 | |
| | | [2 | |
| (a) | M1: for $x = \frac{\log 10}{\log 5}$ or $x = \log_5 10$. Also allow M1 for $x = \frac{1}{\log 5}$ | | |
| | 1.43 with no working (or any working) scores M1A1 (even if left as 5 ^{1.43}). Other answers which round to 1.4 with no working score M1A0. Trial & Improvement Method: M1: For a method of trial and improvement by trialing f(value between 1.4 and 1.43) = Value below 10 and f(value between 1.431 and 1.5) = Value over 10. | | |
| | A1 for 1.43 cao. | | |
| | Note: $x = \log_{10} 5$ by itself is M0; but $x = \log_{10} 5$ followed by $x = 1.430676558$ is M1. | | |
| (b) | M1: Is for correctly eliminating log out of the equation. | | |
| | Eg 1: $\log_3(x-2) = \log_3(\frac{1}{3}) \Rightarrow x-2 = \frac{1}{3}$ only gets M1 when the logs are correctly removed. | | |
| | Eg 2: $\log_3(x-2) = -\log_3(3) \Rightarrow \log_3(x-2) + \log_3(3) = 0 \Rightarrow \log_3(3(x-2)) = 0$ | | |
| | \Rightarrow 3(x-2) = 3° only gets M1 when the logs are correctly removed, | | |
| | but $3(x-2) = 0$ would score M0. | | |
| | Note: $\log_3(x-2) = -1 \Rightarrow \log_3\left(\frac{x}{2}\right) = -1 \Rightarrow \frac{x}{2} = 3^{-1}$ would score M0 for incorrect use | of logs. | |
| | $\frac{\text{Alternative: changing base}}{\log_{10}(x-2)} = -1 \implies \log_{10}(x-2) = -\log_{10}3 \implies \log_{10}(x-2) + \log_{10}3 = 0$ | | |
| | 20810 | | |
| | $\Rightarrow \log_{10} 3(x-2) = 0 \Rightarrow 3(x-2) = 10^{\circ}.$ At this point M1 is scored. | | |