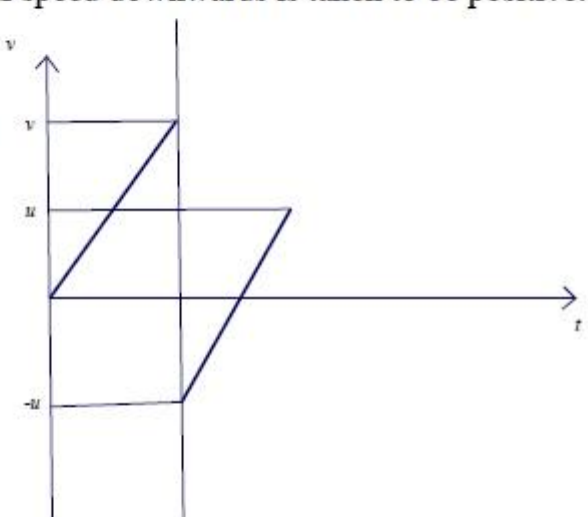


# A level Applied Paper 3B Mechanics Practice Paper M14 **MARK SCHEME**

## Question 1

| Question Number | Scheme  | Marks  |
|-----------------|---|--|
| a               | Using $v^2 = u^2 + 2as$ : $v^2 = 4g$ , $v = \sqrt{4g}$ or 6.3 or 6.26 ( $\text{m s}^{-1}$ )   | M1,A1<br>(2)   |
| b               | Rebounds to 1.5 m, $0 = u^2 - 3g$ , $u = \sqrt{3g}$ , 5.4 or 5.42 ( $\text{m s}^{-1}$ )   | M1A1<br>(2)  |
| c               | Impulse = $0.3(6.3 + 5.4) = 3.5$ (Ns)   | M1A1<br>(2)  |
| d               | <p>If speed downwards is taken to be positive:</p>  <p>First line B1<br/>Second line B1<br/>-u, u, B1</p> <p>(3)</p>  |  |
| e.              | <p>Use of suvat to find <math>t_1</math> or <math>t_2</math>,</p> $\sqrt{4g} = gt_1 \quad t_1 = \sqrt{\frac{4}{g}} = 0.64 \text{ s}$ $\sqrt{3g} = gt_2 \quad t_2 = \sqrt{\frac{3}{g}} = 0.55 \text{ s}$ <p>Total time = <math>t_1 + 2t_2 = 1.7 \text{ s}</math> or 1.75 s</p> | <p>M1A1<br/>(<math>t_1</math> or <math>t_2</math>)</p> <p>DM1A1<br/>(4)<br/>[13]</p> |

### Notes for Question

**N.B.** Deduct only 1 mark in whole question for not giving an answer to either 2 sf or 3 sf, following use of  $g = 9.8$  or use of  $g = 9.81$

#### Question (a)

M1 is for a complete method for finding speed (usually  $v^2 = u^2 + 2as$ )

A1 for  $v = 6.3 \text{ (ms}^{-1}\text{)}$  or  $6.26 \text{ (ms}^{-1}\text{)}$  or  $\sqrt{4g} \text{ (ms}^{-1}\text{)}$  (must be positive)

Allow  $0 = u^2 - 4g$  or  $v^2 = 4g$  but not  $0 = u^2 + 4g$  or  $v^2 = -4g$

#### Question (b)

M1 is for a complete method for finding speed

Allow  $0 = u^2 - 3g$  or  $v^2 = 3g$  but not  $0 = u^2 + 3g$  or  $v^2 = -3g$

A1 for  $5.4 \text{ (ms}^{-1}\text{)}$  or  $5.42 \text{ (ms}^{-1}\text{)}$  or  $\sqrt{3g} \text{ (ms}^{-1}\text{)}$  (must be positive)

#### Question (c)

M1 is for  $\pm 0.3$  (their (b)  $\pm$  their (a)) (unless they are definitely adding the momenta i.e. using  $I = m(v + u)$  which is M0). **N.B.** Extra g is M0

A1 for  $3.5 \text{ (Ns)}$  or  $3.50 \text{ (Ns)}$  (must be positive)

#### Question (d)

First B1 for a straight line from origin to their  $v$  which must be marked on the axis.

Second B1 for a parallel straight line correctly positioned (if continuous vertical lines are clearly included as part of the graph then B0)

Third B1 for their  $-u$  and  $u$  correctly marked, provided their second line is correctly positioned

**N.B.** A reflection of the graph in the  $t$ -axis (upwards +ve) is also acceptable

#### Question (e)

First M1 for use of *suvat* or area under their  $v$ - $t$  graph to find either  $t_1$  or  $t_2$  or  $2t_2$

First A1 for correct value for either  $t_1$  or  $t_2$  (can be in terms of  $g$  at this stage or surds or unsimplified e.g.  $6.3/9.8$ )

Second M1 dependent on the first M1 for their  $t_1 + 2t_2$

Second A1 for  $1.7 \text{ (s)}$  or  $1.75 \text{ (s)}$ .



## Question 2

| Question Number | Scheme   | Marks                                  |
|-----------------|--|--|
| <b>a</b>        | Resolving vertically: $T + 2T (= 3T) = W$<br>Moments about A: $2W = 2T \times d$<br>Substitute and solve: $2W = 2 \frac{W}{3} d$<br>$d = 3$  | M1A1<br>M1A1<br>DM1<br>A1<br>(6)       |
| <b>b</b>        | Resolving vertically: $T + 4T = W + kW \quad (5T = W(1+k))$<br>Moments about A: $2W + 4kW = 3 \times 4T$<br>Substitute and solve: $2W + 4kW = \frac{12}{5} W(1+k)$<br>$2 + 4k = \frac{12}{5} + \frac{12}{5} k$<br>$\frac{8}{5} k = \frac{2}{5}, \quad k = \frac{1}{4}$ | M1A1 ft<br>M1A1 ft<br>DM1<br>A1<br>(6) |
|                 |  | [12]                                   |



### Notes for Question

**N.B.** In moments equations, for the M mark, all terms must be force  $\times$  distance but take care in the cases when the distance is 1.

#### **Question (a)**

**N.B.** If  $Wg$  is used, mark as a misread. *If  $T$  and  $2T$  are reversed, mark as per scheme NOT as a misread.*

First M1 for an equation in  $W$  and  $T$  and possibly  $d$  (either resolve vertically or moments about any point other than the mid-pt), with usual rules.

First A1 for a correct equation.

Second M1 for an equation in  $W$  and  $T$  and possibly  $d$  (either resolve vertically or moments about any point other than the mid-pt), with usual rules.

Second A1 for a correct equation.

Third M1, dependent on first and second M marks, for solving for  $d$

Third A1 for  $d = 3$  cso

**N.B.** If a single equation is used (see below) by taking moments about the mid-point of the rod,  $2T = 2T(d - 2)$ , this scores M2A2 (-1 each error)

Third M1, dependent on first and second M marks, for solving for  $d$

Third A1 for  $d = 3$  cso

#### **Question (b)**

**N.B.** If  $Wg$  and  $kWg$  are used, mark as a misread.

*If they use any results from (a), can score max M1A1 in (b) for one equation.*

*If  $T$  and  $4T$  are reversed, mark as per scheme NOT as a misread.*

First M1 for an equation in  $W$  and a tension  $T_1$  and possibly their  $d$  or their  $d$  and  $k$  (either resolve vertically or moments about any point), with usual rules.

First A1 ft on their  $d$ , for a correct equation.

Second M1 for an equation in  $W$  and **the same tension**  $T_1$  and possibly their  $d$  or their  $d$  and  $k$  (either resolve vertically or moments about any point), with usual rules.

Second A1 ft on their  $d$ , for a correct equation.

Third M1, dependent on first and second M marks, for solving to give a numerical value of  $k$

Third A1 for  $k = 1/4$  oe cso





### Question 3

| Question Number | Scheme  | Marks             |
|-----------------|---|-------------------|
| <b>a</b>        | Resolving horizontally: $T \cos 30^\circ = 6 \cos 50^\circ$<br>$T = 4.45 \text{ (N)}, 4.5 \text{ (N)}, \text{ or better}$ | M1A1<br>A1<br>(3) |
| <b>b</b>        | Resolving vertically: $W = 6 \cos 40^\circ + T \cos 60^\circ$<br>$= 6.82 \text{ (N)}, 6.8 \text{ (N)}, \text{ or better}$ | M1A1<br>A1<br>(3) |
| <b>[6]</b>      |   |                   |

#### Notes for Question

##### Question (a)

First M1 for resolving horizontally with correct no. of terms and both  $T_{AC}$  and '6' terms resolved.

First A1 for a correct equation in  $T_{AC}$  only.

Second A1 for 4.5 (N), 4.45 (N) or better. (4.453363194)

N.B. The M1 is for a complete method to find the tension so where two resolution equations, neither horizontal, are used, the usual criteria for an M mark must be applied to *both* equations and the first A1 is for a correct equation in  $T_{AC}$  *only* (i.e.  $W$  eliminated correctly)

##### Alternatives:

Triangle of Forces :  $\frac{T_{AC}}{\sin 40^\circ} = \frac{6}{\sin 60^\circ}$  (same equation as  $\rightarrow$  resolution) M1A1

Or

Lami's Theorem:  $\frac{T_{AC}}{\sin 140^\circ} = \frac{6}{\sin 120^\circ}$  (same equation as  $\rightarrow$  resolution) M1A1

##### Question (b)

First M1 for resolving vertically with correct no. of terms and both  $T_{AC}$  (does not need to be substituted) and '6' terms resolved.

First A1 for a correct equation in  $T_{AC}$  and  $W$ .

Second A1 for 6.8 (N), 6.82 (N) or better. (6.822948256)

##### Alternatives:

Triangle of Forces :  $\frac{6}{\sin 60^\circ} = \frac{W}{\sin 80^\circ}$  M1A1

Or Lami's Theorem:  $\frac{6}{\sin 120^\circ} = \frac{W}{\sin 100^\circ}$  M1A1

Or Resolution in another direction e.g. along one of the strings M1 (usual criteria) A1 for a correct equation.



#### Question 4

| Question Number | Scheme   | Marks       |
|-----------------|--|-------------|
| (a)             | $R = mg \cos 40$   | B1          |
|                 | Use of $F = \mu R$   | B1          |
|                 | $mg \sin 40 - F = \pm ma$  | M1A1        |
|                 | $acc = 2.55 \text{ (m s}^{-2}\text{)} \text{ or } 2.5 \text{ (m s}^{-2}\text{)}$   | A1<br>(5)   |
| (b)             | $v^2 = u^2 + 2as = 2 \times a \times 3$ Speed at B is $3.9 \text{ (m s}^{-1}\text{)} \text{ or } 3.91 \text{ (m s}^{-1}\text{)}$ | M1A1<br>(2) |
|                 |  | [7]         |

#### Notes for Question

(Deduct only 1 mark in whole question for not giving an answer to either 2 sf or 3 sf, following use of  $g = 9.8$ )

#### Question (a)

First B1 for  $R = mg \cos 40^\circ$

Second B1 for  $F = \mu R$  seen or implied (can be on diagram)

M1 for resolving parallel to plane, correct no. of terms,  $mg$  resolved ( $F$  does not need to be substituted)

First A1 for a correct equation

Second A1 for  $2.5 \text{ (ms}^{-2}\text{)} \text{ or } 2.55 \text{ (ms}^{-2}\text{)}$  Must be **positive**.

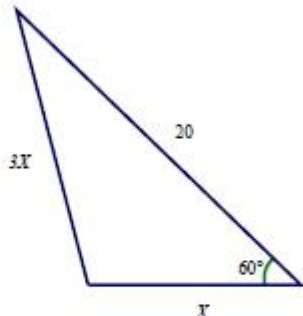
S.C. If  $m$  is given a specific numerical value, can score max B1B1M1A0A0

#### Question (b)

M1 is for a complete method for finding speed (usually  $v^2 = u^2 + 2as$ )

A1 for  $3.9 \text{ (ms}^{-1}\text{)} \text{ or } 3.91 \text{ (ms}^{-1}\text{)}$

# Question 5

| Question Number | Scheme   | Marks                                   |
|-----------------|--|---|
| <b>a</b>        |  <p>Resolve and use Pythagoras<br/> <math>(X - 20\cos 60)^2 + (20\cos 30)^2 = (3X)^2</math></p> $8X^2 + 20X - 400 = 0$ $X = \frac{-5 \pm \sqrt{25 + 800}}{4} = 5.93 \text{ (3 SF)}$ | <p>M1 A1</p> <p>A1<br/>M1A1<br/>(5)</p> |
| <b>a alt</b>    | <p>Cosine rule <math>(3X)^2 = 20^2 + X^2 - 2 \cdot 20 \cdot X \cos 60</math><br/> <math>8X^2 + 20X - 400 = 0</math></p> $X = \frac{-5 \pm \sqrt{25 + 800}}{4} = 5.93 \text{ (3SF)}$  | <p>M1A1<br/>A1</p> <p>M1A1<br/>(5)</p>  |
| <b>b</b>        | $ P - Q ^2 = 20^2 + X^2 - 2X \times 20 \times \cos 120$<br>$ P - Q  = 23.5 \text{ (N) (3SF)}$  | <p>M1A1<br/>DM1 A1<br/>(4)</p>          |
| <b>b alt</b>    | $ P - Q ^2 = (X + 20\cos 60)^2 + (20\cos 30)^2$<br>$ P - Q  = 23.5 \text{ (N) (3SF)}$  | <p>M1A1<br/>DM1 A1<br/>(4)</p>          |
|                 |  | [9]                                     |



### Notes for Question

In this question a misquoted Cosine Rule is M0.

The question asks for both answers to 3 SF but only penalise under or over accuracy once in this question.

#### Question (a)

First M1 for a complete method to give an **equation in  $X$  only** i.e. producing two components *and* usually squaring and adding and equating to  $(3X)^2$  (condone sign errors and consistent incorrect trig. in the components for this M mark **BUT the x-component must be a difference**)

First A1 for a correct unsimplified equation in  *$X$  only*

e.g. allow  $(\pm(X - 20\cos 60^\circ))^2 + (\pm(20\cos 30^\circ))^2 = (3X)^2$

Second A1 for any correct fully numerical *3 term* quadratic = 0

Second M1(**independent**) for solving *a 3 term* quadratic

Third A1 for 5.93

#### **Alternative using cosine rule:**

First M1 for use of cosine rule with  $\cos 60^\circ$  (**M0 if they use  $120^\circ$** )

First A1 for a correct equation unsimplified e.g. allow  $\cos 60^\circ$  and  $(3X)^2$

Second A1 for any correct fully numerical *3 term* quadratic = 0

Second M1(**independent**) for solving *a 3 term* quadratic

Third A1 for 5.93

#### **Alternative using 2 applications of the sine rule:**

First M1 for using  $3X / \sin 60 = X / \sin a$  **AND**

**Either:**  $X / \sin a = 20 / \sin (120^\circ - a)$

**Or:**  $3X / \sin 60^\circ = 20 / \sin (120^\circ - a)$

(These could be in terms of  $b$  where  $b = (120^\circ - a)$ )





First A1 for two correct equations

Second A1 for  $a = 16.778..^\circ$  (or  $b = 103.221..^\circ$ )

Second M1 for solving:

$$X / \sin a = 20 / \sin (120^\circ - a) \text{ or } 3X / \sin 60^\circ = 20 / \sin (120^\circ - a)$$

with their  $a$  or  $b$ , to find  $X$

Third A1 for 5.93

### **Question (b)**

First M1 for use of cosine rule unsimplified with  $\cos 120^\circ$  (M0 if they use  $60^\circ$ )

First A1 for a correct expression for  $|P - Q|$  in terms of  $X$  (does not need to be substituted)

Second M1, **dependent on first M1**, for *substituting for their  $X$  and solving for  $|P - Q|$*

Second A1 for 23.5

**Alternative using components:**

First M1 for a complete method i.e. producing two components *and* squaring and adding (no square root needed) (condone sign errors and consistent incorrect trig. in the components for this M mark

**BUT the x-component must be a sum)**

First A1 for a correct expression for  $|P - Q|$

(e.g. allow  $(\pm(X + 20\cos 60^\circ))^2 + (\pm(20\cos 30^\circ))^2$ )

Second M1, **dependent on first M1**, for *substituting for their  $X$  and solving for  $|P - Q|$*

Second A1 for 23.5



## Question 6

| Question Number    | Scheme   | Marks                   |
|--------------------|--|-------------------------|
| a                  | $\mathbf{F} = m\mathbf{a}: 3\mathbf{i} - 2\mathbf{j} = 0.5\mathbf{a}$<br>$\mathbf{a} = 6\mathbf{i} - 4\mathbf{j}$<br>$ \mathbf{a}  = \sqrt{6^2 + (-4)^2} = 2\sqrt{13} (\text{m s}^{-2})^{**}$  | M1<br>A1<br>M1A1<br>(4) |
| b                  | $\mathbf{v} = \mathbf{u} + \mathbf{at}: \mathbf{v} = (\mathbf{i} + 3\mathbf{j}) + 2(6\mathbf{i} - 4\mathbf{j})$<br>$= 13\mathbf{i} - 5\mathbf{j} \text{ m s}^{-1}$   | M1A1 ft<br>A1<br>(3)    |
| c                  | Distance = $2 \mathbf{v}  = 2\sqrt{4+1} = 2\sqrt{5} = 4.47 \text{ (m)}$  | M1A1<br>(2)             |
| d                  | When $t = 3.5$ , velocity of $P$ is $(\mathbf{i} + 3\mathbf{j}) + 3.5(6\mathbf{i} - 4\mathbf{j}) = 22\mathbf{i} - 11\mathbf{j}$<br>Given conclusion reached correctly. E.g. $22\mathbf{i} - 11\mathbf{j} = 11(2\mathbf{i} - \mathbf{j})$ | M1A1 ft<br>A1<br>(3)    |
| Notes for Question |  | [12]                    |



### Question (a)

**Either:**

First M1 for use of  $F = m a$

First A1 for  $a = 6i - 4j$

Second M1 for  $a = \sqrt{6^2 + (-4)^2}$  (Allow  $\sqrt{6^2 + 4^2}$ )

Second A1 for  $a = 2\sqrt{13} \text{ (ms}^{-2}\text{)}$  **Given answer**

**Or:**

First M1 for  $F = \sqrt{3^2 + (-2)^2}$  (Allow  $\sqrt{3^2 + 2^2}$ )

First A1  $F = \sqrt{13}$

Second M1 for  $\sqrt{13} = 0.5 a$

Second A1 for  $a = 2\sqrt{13} \text{ (ms}^{-2}\text{)}$  **Given answer**

### Question (b)

M1 for  $(i + 3j) + (2 \times \text{their } a)$

First A1 ft for a correct expression

Second A1 for  $13i - 5j$ ; isw if they go on to find the speed

### Question (c)

M1 for  $2\sqrt{2^2 + (-1)^2}$  or  $\sqrt{4^2 + (-2)^2}$

A1 for  $2\sqrt{5}$  or  $\sqrt{20}$  or 4.5 or 4.47 or better

### Question (d)

M1 for  $(i + 3j) + (3.5 \times \text{their } a)$ , or possibly, their (b) + (1.5 x their a)

First A1 ft for a correct expression *of form*  $ai + bj$

Second A1 for given conclusion reached correctly *e.g.*  $22i - 11j = 11(2i - j)$  oe **Given answer**



# Question 7

| Question Number   | Scheme   | Marks               | Notes   |
|---|--|---------------------|---|
| (a)   | Resolving vertically: $Y + P \cos \theta = W$  | M1                  | Needs all 3 terms. Condone sign errors and sin/cos confusion. Condone $Wg$<br><br>Terms need to be of the correct structure, but condone $l$ implied if not seen.<br><br>Substitute for $P$ to obtain simplified $Y$<br>Requires both preceding M marks<br>Obtain <b>given result</b> correctly.                      |
|   | Moments about $A$ : $Wl \cos \theta = 2lP$   | A1                  |   |
|   | $P = \frac{W \cos \theta}{2} \Rightarrow Y = W - \frac{W \cos^2 \theta}{2} = \frac{W}{2}(2 - \cos^2 \theta)$<br>** | M1<br>A1<br>DM1     |   |
|   | NB $W + Y = P \cos \theta$ with correct conclusion is possible   | A1 (6)              |   |
| They need to find two independent equations that do not include $X$ . If they have equations involving $X$ they need to attempt to eliminate $X$ before they score any marks  |  |                     |   |
| (b)   | $\theta = 45^\circ \Rightarrow Y = \frac{3W}{4}$   | B1                  | Resolving horizontally. Accept in terms of $\theta$ .<br>Express $X$ in terms of $W$ .<br>Accept in terms of $\theta$ .<br>Requires preceding M mark.<br>Correct unsimplified but substituted.<br>Use of Pythagoras with $X, Y$ in terms of $W$ only. Dependent on the first M1<br>Or equivalent ( $0.79W$ or better) |
|   | $X = P \sin 45$  | M1                  |   |
|   | $= \frac{W \cos 45}{2} \cdot \sin 45 \left( = \frac{W}{4} \right)$   | DM1                 |   |
|   | Resultant at $A = \frac{W}{4} \sqrt{3^2 + 1^2} = \frac{W\sqrt{10}}{4}$<br>( $0.79W$ )                              | A1<br>DM1<br>A1 (6) |   |
| Alternative moments equations: about the centre $P l + X \sin \theta l = y \cos \theta l$<br>About the point where the lines of action of $P$ and $X$ intersect $Y \times \frac{2l}{\cos \theta} = W \left( \frac{2l}{\cos \theta} - l \cos \theta \right)$ |  |                     |   |





## Question 8

| Question Number | Scheme   | Marks                   |
|-----------------|--|-------------------------|
| (a)             | $4mg - T = 4ma$  | M1A1                    |
|                 | $T - 3mg = 3ma$  | M1A1                    |
|                 | Condone the use of $4mg - 3mg = 4ma + 3ma$ in place of one of these equations.   | M1A1                    |
|                 | Reach given answer $a = \frac{g}{7}$ correctly ***   | A1                      |
|                 | Form an equation in $T$ :<br>$T = 3mg + 3\left(mg - \frac{T}{4}\right)$ , $T = 3mg + 3m\frac{g}{7}$ , or $T = 4mg - 4m\frac{g}{7}$ | M1                      |
|                 | $T = \frac{24}{7}mg$ or equivalent, $33.6m$ , $34m$  | A1<br>(7)               |
| (b)             | $v^2 = u^2 + 2as = 2 \times \frac{g}{7} \times 0.7 = 1.96$ , $v = 1.4 \text{ ms}^{-1}$   | M1A1<br>(2)             |
| (c)             | $3mg - T = 3ma$<br>$T - 2mg = 2ma$<br>$a = \frac{g}{5}$  | M1A1<br>A1<br>A1<br>(4) |
| (d)             | $0 = 1.96 - 2 \times \frac{g}{5} \times s$   | M1                      |
|                 | $s = \frac{5 \times 1.96}{2g} = 0.5 \text{ (m)}$   | A1                      |
|                 | Total height = $0.7 + 0.5 = 1.2 \text{ (m)}$   | A1 ft<br>(3)            |
| Alt d           | Using energy: $3mgs - 2mgs = \frac{1}{2}3m \times 1.4^2 + \frac{1}{2}2m \times 1.4^2$  | M1                      |
|                 | $s = \frac{2.5 \times 1.96^2}{g} = 0.5 \text{ (m)}$  | A1                      |
|                 | Total height = $0.7 + 0.5 = 1.2 \text{ (m)}$   | A1 ft<br>(3)            |
|                 |  | [16]                    |



### Notes for Question

#### Question (a)(i) and (ii)

First M1 for resolving vertically (up or down) for  $B+C$ , with correct no. of terms.

First A1 for a correct equation.

Second M1 for resolving vertically (up or down) for  $A$ , with correct no. of terms.

Second A1 for a correct equation.

Third A1 for  $g/7$ , obtained correctly. **Given answer (1.4 A0)**

Third M1 for an equation in  $T$  only

Fourth A1 for  $24mg/7$  oe or  $33.6m$  or  $34m$

**N.B.** If they omit  $m$  throughout (which gives  $a = g/7$ ), can score max M1A0M1A0A0M1A0 for part (a) BUT CAN SCORE ALL OF THE MARKS in parts (b), (c) and (d).

#### Question (b)

M1 for an equation in  $v$  only (usually  $v^2 = u^2 + 2as$ )

A1 for  $1.4 \text{ (ms}^{-1}\text{)}$  allow  $\sqrt{(g/5)}$  oe.

#### Question (c)

First M1 for resolving vertically (up or down) for  $A$  or  $B$ , with correct no. of terms. (**N.B.** M0 if they use the tension from part (a))

First A1 for a correct equation for  $A$ .

Second A1 for a correct equation for  $B$ .

**N.B.** 'Whole system' equation:  $3mg - 2mg = 5ma$  earns first 3 marks but any error loses all 3

Third A1 for  $g/5$  oe or  $1.96$  or  $2.0 \text{ (ms}^{-2}\text{)}$  (allow a negative answer)

#### Question (d)

M1 for an equation in  $s$  only using their  $v$  from (b) and  $a$  from (c).

either  $0 = 1.4^2 - 2(g/5)s$  or  $1.4^2 = 0 + 2(g/5)s$

First A1 for  $s = 0.5 \text{ (m)}$  correctly obtained

Second A1 ft for their  $0.5 + 0.7 = 1.2 \text{ (m)}$

#### **Alternative using conservation of energy**

M1 for an equation in  $s$  only, with correct number of terms, using their  $v$  from (b):-

$(3mgs - 2mgs) = \frac{1}{2} 3m (1.4)^2 + \frac{1}{2} 2m (1.4)^2$

First A1 for  $s = 0.5 \text{ (m)}$  correctly obtained

Second A1 ft for their  $0.5 + 0.7 = 1.2 \text{ (m)}$

### Question 9

| Question Number  | Scheme   | Marks     | Notes  |
|--|--|-----------|--|
| (a)  | Integrate: $\mathbf{v} = (t^3 - 2t^2)\mathbf{i} + (3t^2 - 5t)\mathbf{j} + \mathbf{C}$<br><br>$t = 3 : \mathbf{v} = 9\mathbf{i} + 12\mathbf{j} + \mathbf{C} = 11\mathbf{i} + 10\mathbf{j}$<br>$\mathbf{C} = 2\mathbf{i} - 2\mathbf{j}$<br>$\mathbf{v} = (t^3 - 2t^2 + 2)\mathbf{i} + (3t^2 - 5t - 2)\mathbf{j}$ | M1        | At least 3 powers going up. Condone errors in constants. Must be two separate component equations if not in vector form.<br>Could be in column vector form.<br>Allow with no "+ C" |
|  |  | A2        | -1 each integration error. i.e. All correct A1A1<br>1 error A1A0, 2 or more errors A0A0<br>Allow with no "+ C"   |
|  |  | DM1       | Substitute given values to find C.<br>Dependent on the previous M mark   |
|  |  | A1<br>(5) | Correct velocity (any equivalent form)   |
| (b)  | Parallel to $\mathbf{i} \Rightarrow 3t^2 - 5t - 2 = 0$<br><br>$(3t+1)(t-2) = 0,$<br>$t = 2$<br><br>$ \mathbf{v}  = 8 - 8 + 2 = 2 \text{ (m s}^{-1}\text{)}$  | M1        | Set $\mathbf{j}$ component of their $\mathbf{v}$ equal to zero and solve for $t$ . Correct answers imply method, but incorrect answers need to show method clearly.                |
|  |  | A1        | Correct only. Ignore $-\frac{1}{3}$ if present.  |
|  |  | DM1       | Substitute their $t$ to find $\mathbf{v}$ .<br>Dependent on the previous M mark.   |
|  |  | A1<br>(4) | The <b>answer must be a scalar</b> – the Q asks for speed. Results from negative $t$ must be rejected.   |
|  |  | [9]       |  |
| A candidate who has no "+C" can score at most<br>M1A2M0A0 M1A0M1A0 |  |           |  |



# Question 10

| Question Number | Scheme  | Marks   | Notes  |
|-----------------|---|---|--|
| (a)             | <p>Considering energy:</p> $\frac{1}{2}m \times 14^2 = \frac{1}{2}m \times 10^2 + mgh$ $h = \frac{48}{g} = 4.90$  | <p>M1</p> <p>A2</p> <p>A1</p> <p>(4)</p>  | <p>All terms required. Terms need to be of the correct form but condone sign errors.</p> <p>-1 each error in the unsimplified equation</p> <p>Accept <math>\frac{48}{g}</math>. Maximum 3 s.f. if they go in to decimals.</p>  |
| alt(a)          | <p>Initial <math>v_y = 14 \sin \alpha</math> Final</p> $v_y = \sqrt{100 - 14^2 \cos^2 \alpha}$ $100 - 196 \cos^2 \alpha = 196 \sin^2 \alpha - 2gh$ $h = \frac{48}{g} = 4.90$  | <p>M1A2</p> <p>A1</p> <p>(4)</p>  | <p>Using <math>v^2 = u^2 + 2as</math> on the vertical components of speed.</p> <p>-1 each error in the unsimplified equation</p> <p>Accept in exact form. Maximum 3 s.f. if they go in to decimals.</p>  |
| NB              | Using $v^2 = u^2 + 2as$ with 10 and 14 is M0  |   |  |
| NB              | In part (a) they must be solving the general case, not using 0.85. However, the marks in (b) are all available if they solve the specific case in (a).  |   |  |
| (b)             | <p>Vertical distance: <math>h = 14 \sin \alpha t - \frac{1}{2} \times 9.8 t^2</math></p> $4.9 t^2 - 11.9 t + h = 0$ $t = \frac{11.9 \pm \sqrt{11.9^2 - 4 \times 4.9^2}}{9.8}$ $t = 1.903 \dots$ <p>Horizontal distance: <math>x = 14 \cos \alpha \times t</math></p> $= 14.0 \text{ (m)}$ | <p>M1</p> <p>A2</p> <p>DM1</p> <p>A1</p> <p>M1</p> <p>A1</p> <p>A1</p> <p>(8)</p> | <p>A complete method to find an equation in <math>t</math>. Must involve trig condone sin/cos confusion</p> <p>Correct in <math>h</math> or their <math>h</math>. -1 each error</p> <p>Solve a 3 term quadratic for <math>t</math>.</p> <p>Needs their value for <math>h</math> now.</p> <p>1.9 or better</p> <p>Method for the horizontal distance.</p> <p>Condone consistent sin/cos confusion</p> <p>Correct for their positive <math>t</math></p> <p>Accept 14</p> |
| Alt (b)         | <p>Vertical speed = <math>\sqrt{100 - (14 \cos \alpha)^2} (=6.75)</math></p> $v = u + at = 14 \times 0.85 - 9.8t$ $(-6.75 = 11.9 - 9.8t)$ $t = 1.903 \dots$ <p>Horizontal distance: <math>x = 14 \cos \alpha \times t</math></p> $= 14.0 \text{ (m)}$                                     | <p>M1</p> <p>A2</p> <p>DM1</p> <p>A1</p> <p>M1</p> <p>A1</p> <p>A1</p> <p>(8)</p> | <p>A complete method to find the vertical component of the speed at B.</p> <p>Correct insimplified. -1 each error.</p> <p>Use their vertical component to find <math>t</math></p> <p>1.9 or better</p> <p>Method for the horizontal distance.</p> <p>Correct for their positive <math>t</math></p> <p>Accept 14</p>  |
|                 |   | [12]  |  |
| NB              | Candidates with a false method leading to 4.9 in (a) score at most M1A1A1DM1A0M1A1A0 if they use their result in (b). This error does not affect the alt (b) approach   |   |  |