Name:....

Total Marks:....



## Instructions

- Use **black** ink or ball-point pen.
- Fill in the boxes at the top of this page with your name.
- Answer **all** questions.
- Answer the questions in the spaces provided
  there may be more space than you need.
- Show all your working out

## Information

- The total mark for this paper is 148.
- The marks for **each** question are shown in brackets.
  - use this as a guide as to how much time to spend on each question.
- Questions labelled with an **asterisk** (\*) are ones where the quality of your written communication will be assessed

## Advice

- Read each question carefully before you start to answer it
- Attempt every question
- Check your answers if you have time at the end



1.	Functions f and g is such that $f(x) = 2x - 1$ and $g(x) = \frac{3}{x}$	
	<ul><li>(a) Find the value of</li><li>(i) f(3)</li></ul>	
	(ii) fg(6)	(1)
	(b) $f^{-1}(x) =$	(2)
	(c) $gf(x) =$	(2)
		(2)

2. The function f is such that f(x) = 4x - 1(a) Find  $f^{-1}(x)$ 

......(2)

The function g is such that  $g(x) = kx^2$  where k is a constant. (b) Given that fg(2) = 12, work out the value of k



3. Functions f and g are such that f(x) = 3(x-4) and  $g(x) = \frac{x}{5} + 1$ (a) Find the value of f(10)

.....(1)

(b) Find  $g^{-1}(x)$ 

(c) Show that ff(x) = 9x - 48

......(2)

4. Given that  $f(x) = x^2$  and g(x) = x - 6, solve the equation  $fg(x) = g^{-1}(x)$ 



- 5. f and g are functions such that f(x) = 2x 3 and  $g(x) = 1 + \sqrt{x}$ 
  - (a) Calculate f(-4)

......(1)

(b) Given that f(a) = 5, find the value of *a*.

(c) Calculate gf(6).

......(2)

......(2)

(d) Find the inverse function  $g^{-1}(x)$ .



**6.** Functions f and g are such that

$$f(x) = \frac{1}{x+2}$$
 and  $g(x) = \sqrt{x-1}$ 

(a) Calculate fg(10)

......(2)

(b) Find the inverse function  $g^{-1}(x)$ .



- 7. Functions f and g are such that f(x) = 2x + 2 and  $g(x) = 2x^2 - 5$ 
  - (a) Find the composite function fg. Give your answer as simply as possible.

......(2)

(b) Find the inverse function  $f^{-1}(x)$ .

......(2)

(c) Hence, or otherwise, solve  $f^{-1}(x) = g^{-1}(x)$ .



8. The function f is such that 
$$f(x) = \frac{1}{x+3}$$

(a) Find the value of f(2)

.....(1)

(b) Given that 
$$f(a) = \frac{1}{10}$$
, find the value of *a*.

......(2)

The function g is such that g(x) = x + 2

(c) Find the function gf.

Give your answer as a single algebraic fraction in its simplest form.



- 9. Functions f and g are such that  $f(x) = x^2$  and g(x) = x 3
  - (a) Find gf(x).

......(2)

(b) Find the inverse function  $g^{-1}(x)$ .

(c) Solve the equation  $gf(x) = g^{-1}(x)$ .



- **10.** The function f is such that  $f(x) = (x 1)^2$ 
  - (a) Find f(8)

......(1)

The function g is such that  $g(x) = \frac{x}{x-1}$ (b) Solve the equation g(x) = 1.2

......(3)

(c) (i) Express the inverse function  $g^{-1}$  in the form  $g^{-1}(x) =$ 

(ii) Hence write down gg(x) in terms of x.



- 11. f is a function such that  $f(x) = \frac{1}{x^2 + 1}$ 
  - (a) Find  $f(\frac{1}{2})$

.....(1)

g is a function such that  $g(x) = \sqrt{x-1}$ ,  $x \ge 1$ 

(b) Find fg(x)Give your answer as simply as possible.



12. The function f is such that  $f(x) = \frac{x-6}{2}$ (a) Find f(8)

(b) Express the inverse function  $f^{-1}$  in the form  $f^{-1}(x) =$ 

The function g is such that  $g(x) = \sqrt{x-4}$ 

(c) Express the function gf in the form gf(x) = Give your answer as simply as possible.



13. Functions f and g are such that f(x) = 3x - 2 and  $g(x) = \frac{10}{x+2}$ (a) Express the inverse function f<sup>-1</sup> in the form f<sup>-1</sup>(x) =

......(2)

(b) Find gf(x)Simplify your answer.



- 14. Functions f and g are such that  $f(x) = \frac{2}{x}$  and  $g(x) = \frac{x+1}{x}$ 
  - (a) Solve gf(a) = 3

......(3)

(b) Express the inverse function  $g^{-1}$  in the form  $g^{-1}(x) =$ 



15. Functions g and h are such that  $g(x) = \frac{x}{2x-5}$  and h(x) = x+4(a) Find the value of g(1)

.....(1)

(b) Find gh(x)Simplify your answer.

.....(2)

(c) Express the inverse function  $g^{-1}$  in the form  $g^{-1}(x) =$ 



16. The function f is such that  $f(x) = \frac{1}{x+4}$ ,  $x \neq -4$ . Evaluate f<sup>-1</sup>(3).

......(3)

17. Given that f(x) = 3x - 1,  $g(x) = x^2 + 4$  and fg(x) = gf(x),

show that  $x^2 - x - 1 = 0$ 

.....(5)



**18.** Functions f and g are such that

$$f(x) = 3x + 2$$
  $g(x) = x^2 + 1$ 

Find an expression for  $(fg)^{-1}(x)$ 

.....(3)

- **19.** The function f is such that  $f(x) = \frac{8}{x+2}$ 
  - (a) Find  $f^{-1}(x)$ .

(b) Solve the equation  $f^{-1}(x) = f(x)$ 



20. The function g is such that  $g(x) = \frac{1}{1-x}$  for  $x \neq 1$ (a) Prove that  $gg(x) = \frac{x-1}{x}$ 

......(3)

(b) Find ggg(3)



**21.** Functions f, g and h are such that f(x) = 3 - x,  $g(x) = x^2 - 14$  and h(x) = x - 2Given that f(x) = gfh(x), find the values of x.

......(5)

22. The function f is defined by  $f(x) = \frac{x-1}{x}, x \neq 0$ Solve ff(x) = -2



**23.** 
$$f(x) = \frac{x}{x+3}, x \in \mathbb{R}, x \neq -3$$

(a) If  $f^{-1}(x) = -5$ , find the value of *x*.

......(3)

(b) Show that  $\text{ff}^{-1}(x) = x$ 



24. 
$$f(x) = \frac{x}{x+3}, x \in \mathbb{R}, x \neq -3$$
  
(a) If  $f^{-1}(x) = -5$ , find the value of x.

......(3)

(b) Show that  $\operatorname{ff}^{-1}(x) = x$ 



## **25.** f(x) = 2x + c

g(x) = cx + 5

$$fg(x) = 6x + d$$

c and d are constants.

Work out the value of d.

......(3)

**26.**  $f(x) = 3x^2 - 2x - 8$ 

Express f(x + 2) in the form  $ax^2 + bx$ 



**27.**  $f(x) = x^2 - 2x - 4$ 

Express f(2x - 1) in the form  $ax^2 + bx + c$ 

......(3)

**28.**  $f(x) = x^2 + 3x + 4$ 

Show that f(x - 2) - f(x) = -4x - 2

......(3)

**TOTAL FOR PAPER: 148 MARKS**